

# Options for Mitigation Measures

Avenues for new research

**Enrique Mallada**  
Associate Professor, ECE

ESIG/G-PST Special Topic Workshop  
March 28, 2024

# Grid Team at ROSEI



**Benjamin Hobbs**  
Theodore M. and Kay  
W. Schad Professor  
JHU-EHE, ROSEI



**Dennice Gayme**  
Associate Professor  
JHU-ME, ROSEI



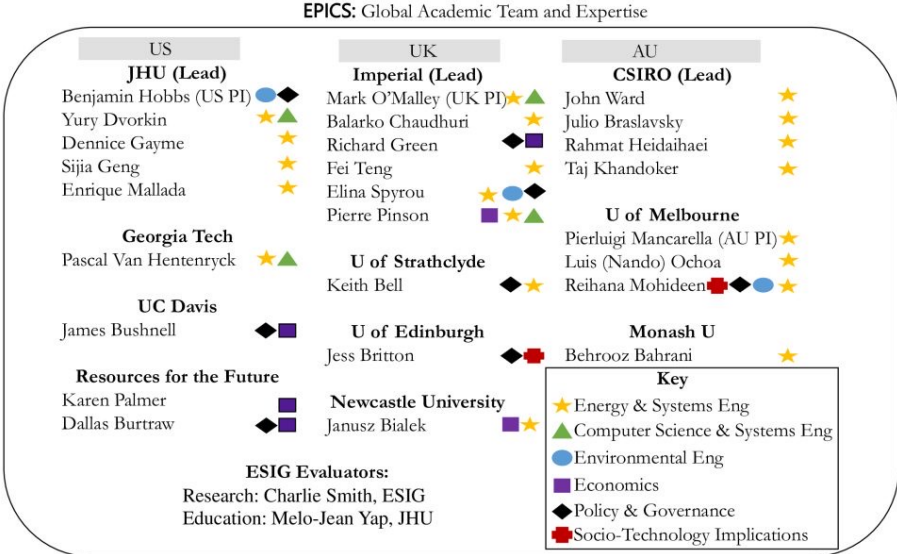
**Enrique Mallada**  
Associate Professor  
JHU-ECE, ROSEI



**Yury Dvorkin**  
Associate Professor  
JHU-ECE/CSE, ROSEI



**Sijia Geng**  
Assistant professor  
JHU-ECE, ROSEI



NSF Global Center: EPICS  
Electric Power Innovation for a Carbon-free Society

# Outline

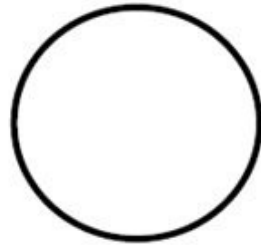
- A Word of Caution: GFM IBRs Complex Dynamics
  - Faster controls **can speed up the transition to chaos**
- Decentralized Stability Analysis in Power Grids
  - Generalizing control tools for network systems
- Avenues for Future Research
  - Early detection via critical slow-down
  - Novel IBR control designs: Trading Freq. vs Volt. Support
  - The role of operations in SSO prevention





# Nonlinear Phenomena in IBR-rich Grids

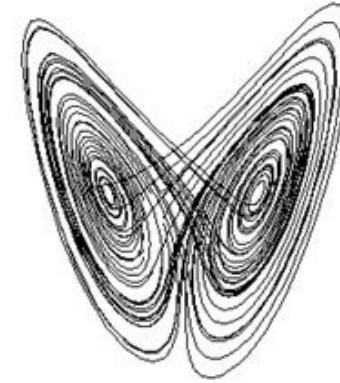
Sustained oscillatory behavior is intrinsically **nonlinear phenomena** induced by **bifurcations** which often can leads to **chaos**



limit cycle



limit torus



chaotic attractor

Prior art (1989<sup>[1]</sup> – 2004<sup>[2]</sup>) focus on nonlinear phenomena induced by synchronous machines.

## Three well-known routes to chaos<sup>[3]</sup>:

- **Period-doubling** route: doubling of subsequent periodicities.
- Ruelle-Takens-Newhouse **quasi-periodicity route**: quasi-periodic torus attractors.
- Maneville-Pomeau **intermittency route**: sudden bursts to chaos.

[1] I Dobson, H.-D. Chiang, *Towards a theory of voltage collapse in electric power systems*. Systems & Control Letters 1989

[2] J. Hongjie et al, *Three routes to chaos in power systems*. Canadian Conference on Electrical and Computer Engineering 2004

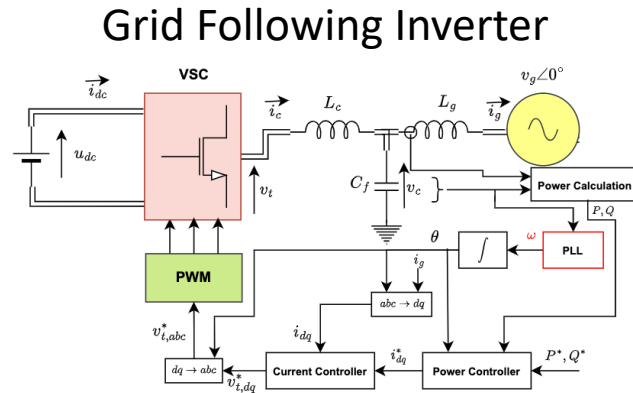
[3] Abraham, Arimondo, and Boyd, *Instabilities, dynamics and chaos in nonlinear optical systems*.



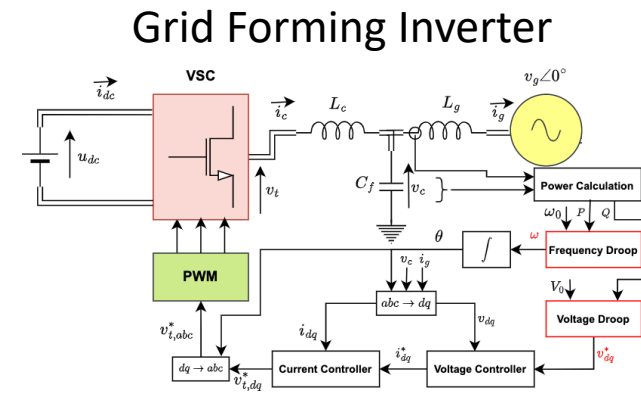
# Nonlinear Phenomena in IBR-rich Grids

Q1: Can IBR-rich power grids induce chaotic behavior?

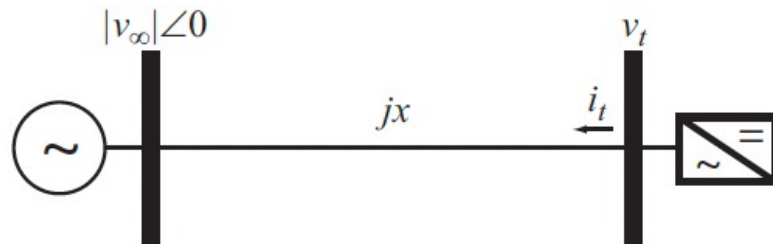
Q2: Is there a fundamental difference between GFL and GFL Inverters?



VS

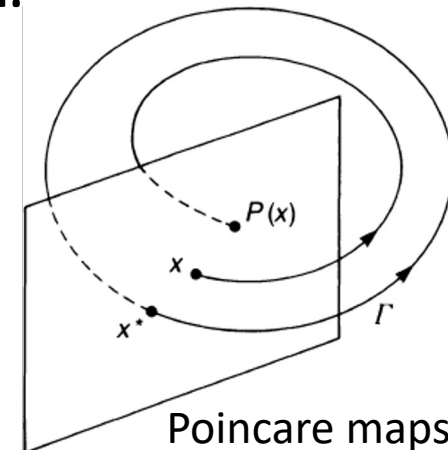


## Problem Setup:



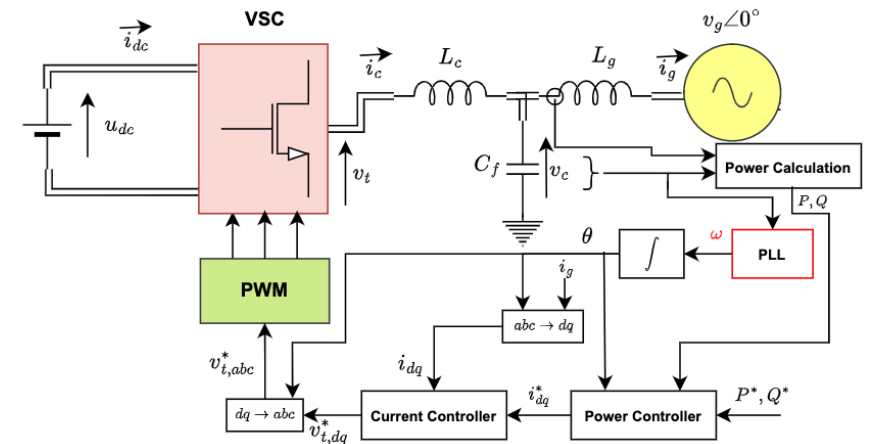
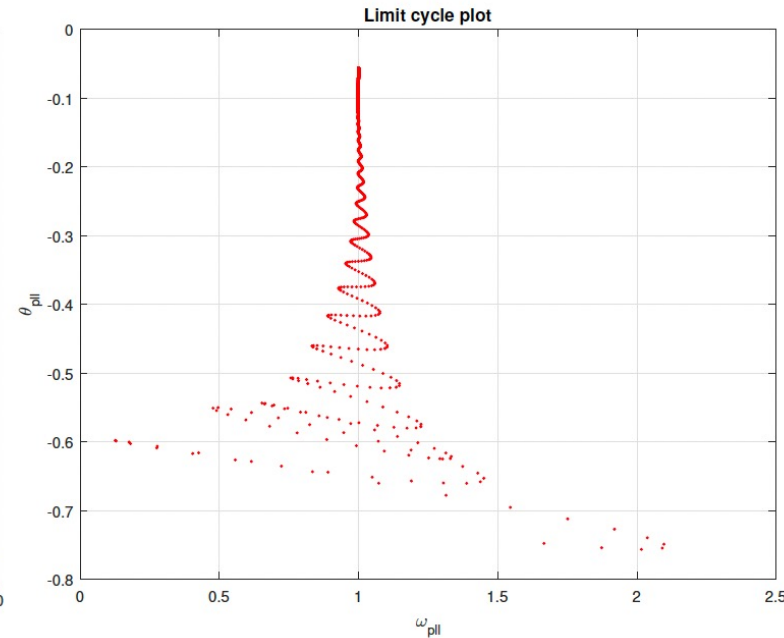
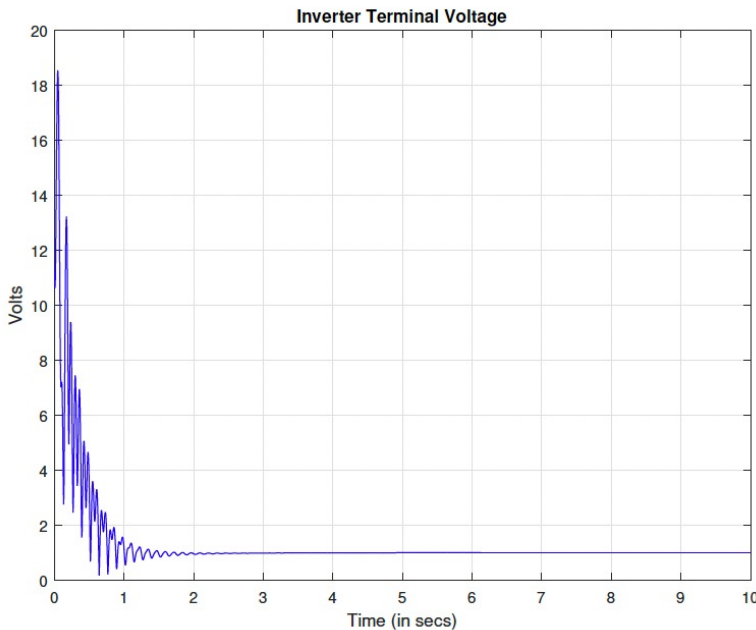
- IBR connected to infinite bus
- Use current controller gain  $K_p$  as bifurcation parameter

## Analysis Tool:



# GFL Inverter

Case 1: Normal Operation ( $K_p = 1.5$ )  $\Rightarrow$  Fixed Point

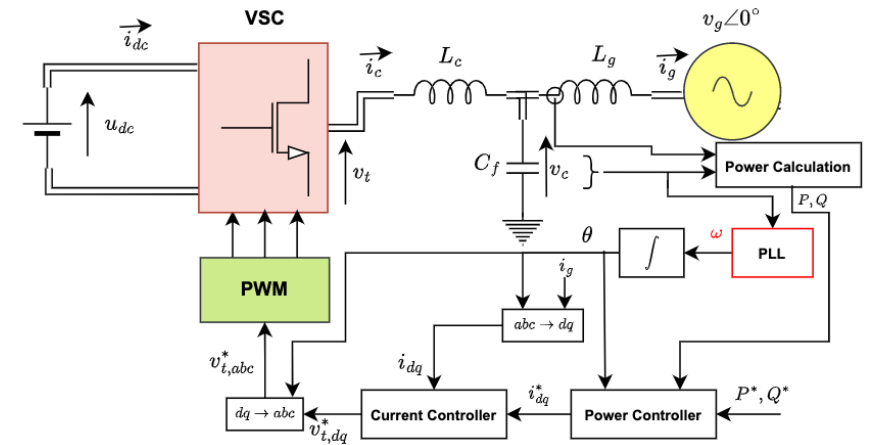
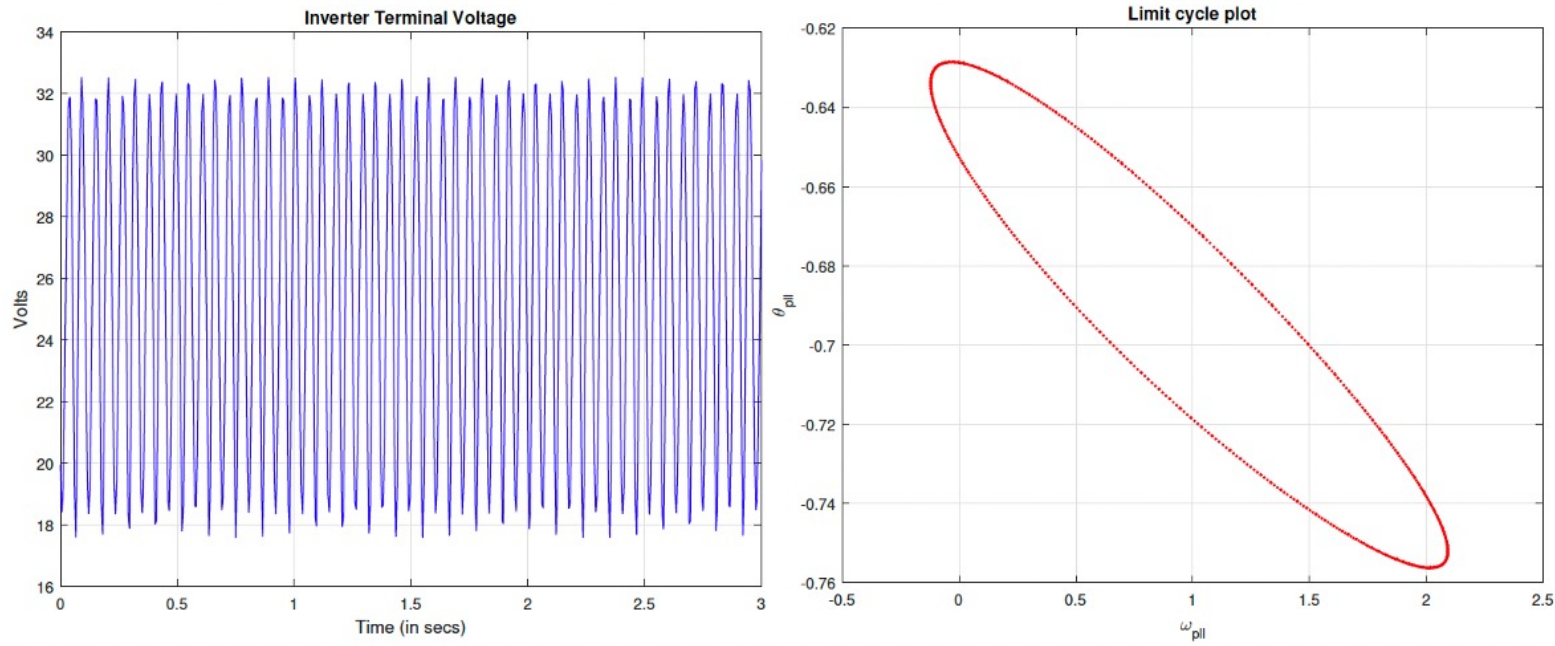


Bifurcation parameter is chosen as the proportional gain  $K_p$  of the current controller.



# GFL Inverter

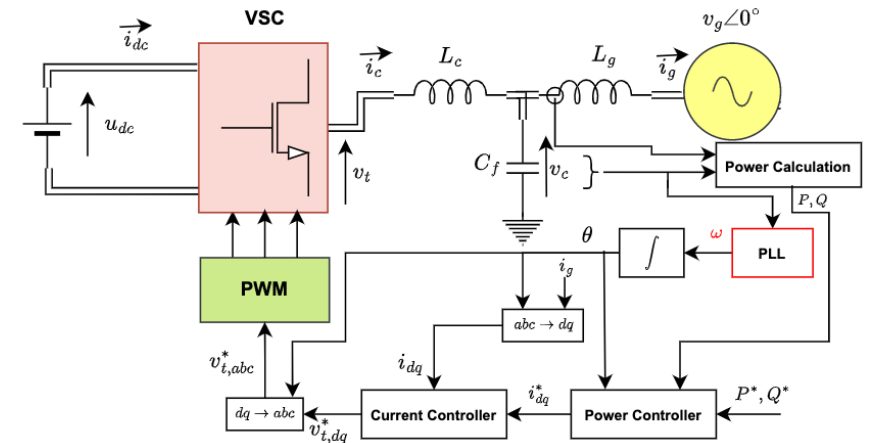
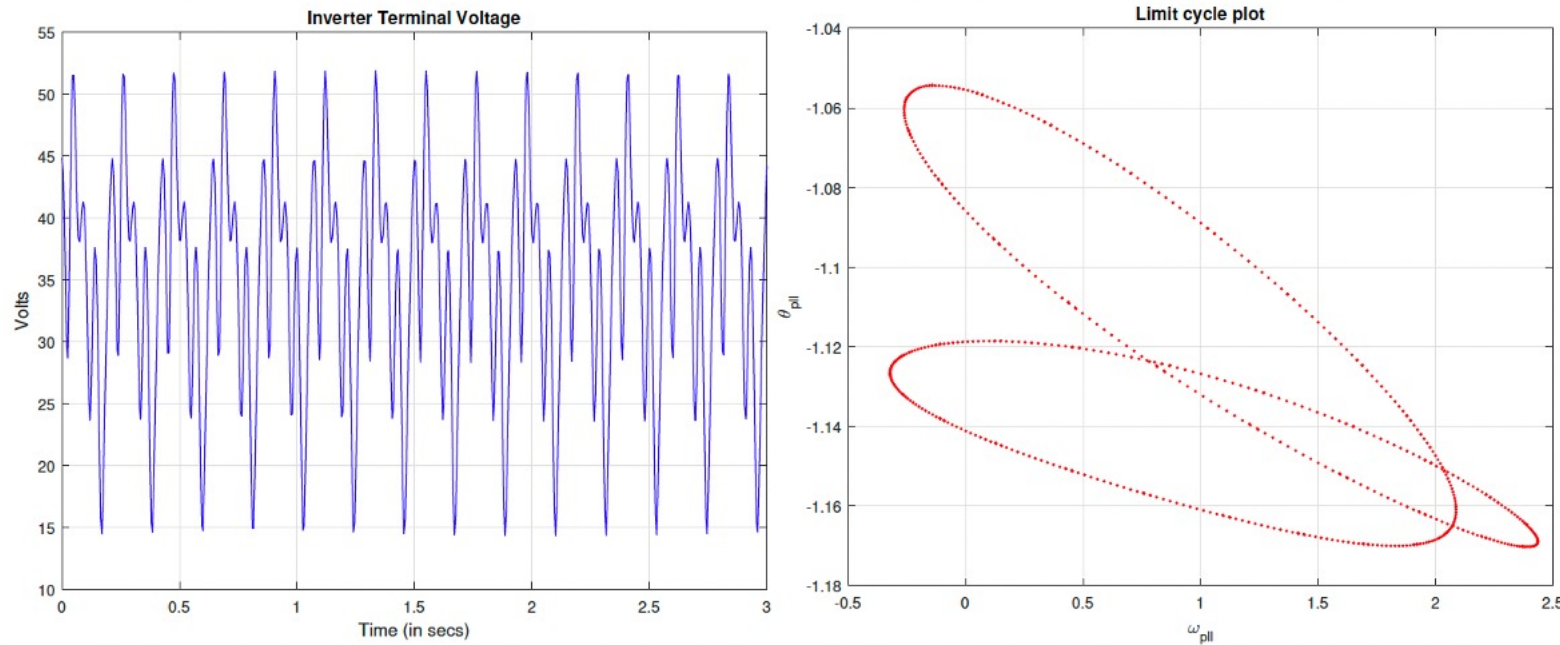
Case 2: ( $K_p = 3.0$ )  $\Rightarrow$  Period-1 Orbit ( $T=0.115s$ )



Bifurcation parameter is chosen as the proportional gain  $K_p$  of the current controller.

# GFL Inverter

Case 3: ( $K_p = 5$ )  $\Rightarrow$  Period-2 Orbit ( $T=0.215s$ )

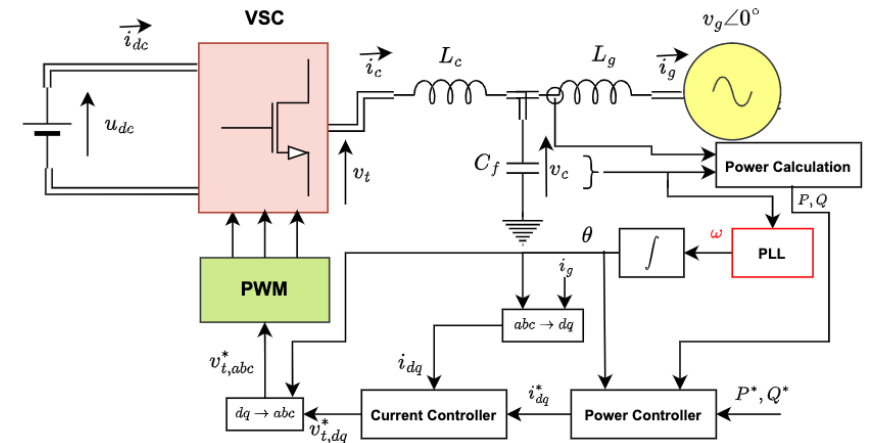
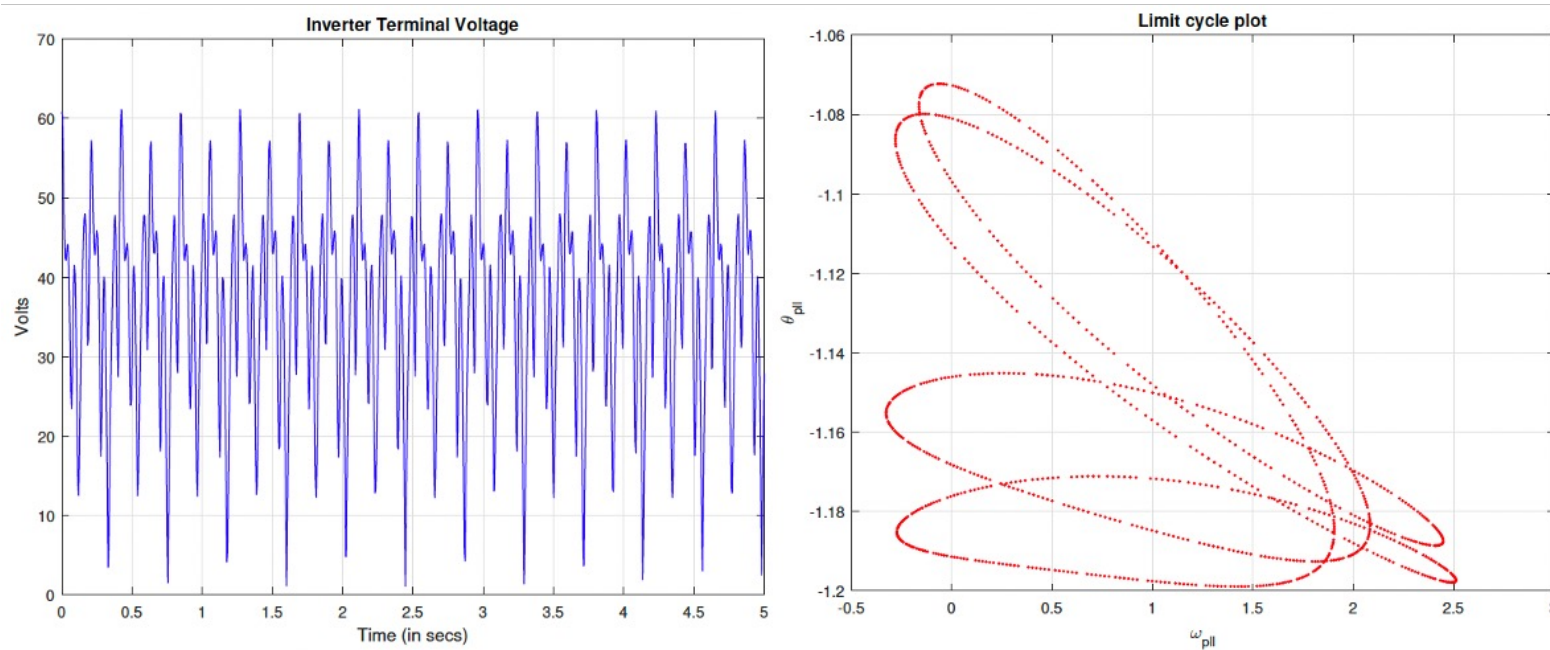


Bifurcation parameter is chosen as the proportional gain  $K_p$  of the current controller.



# GFL Inverter

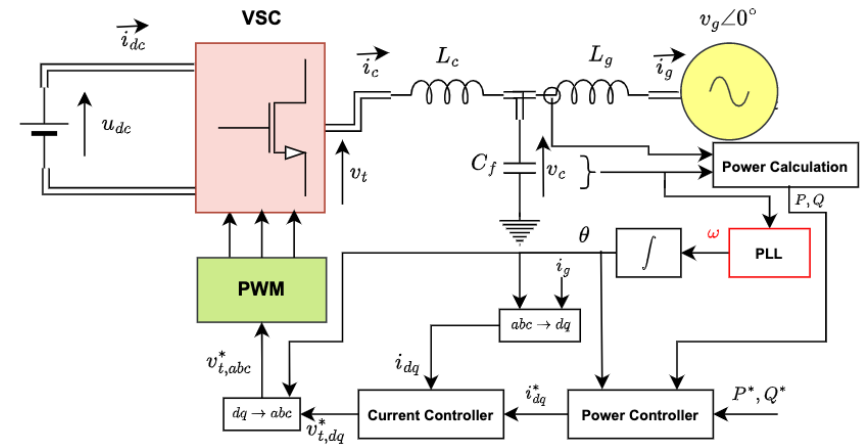
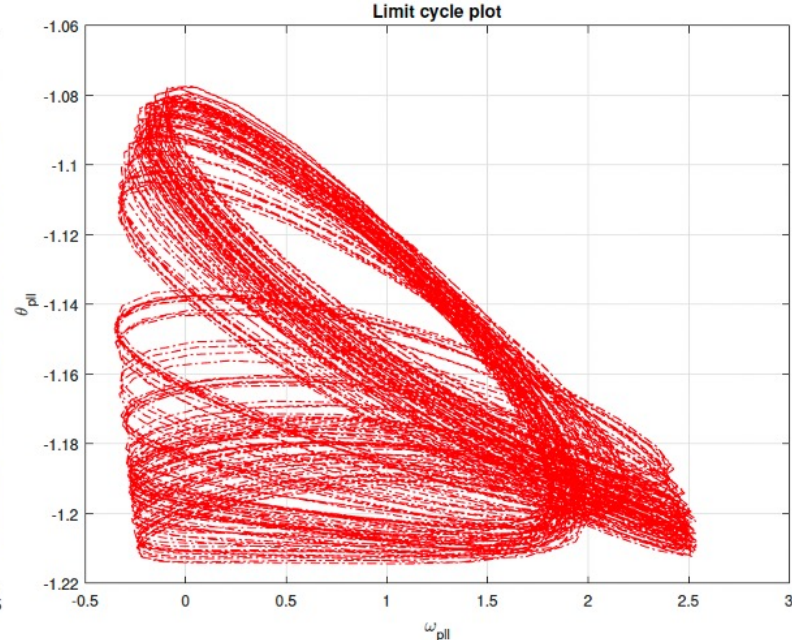
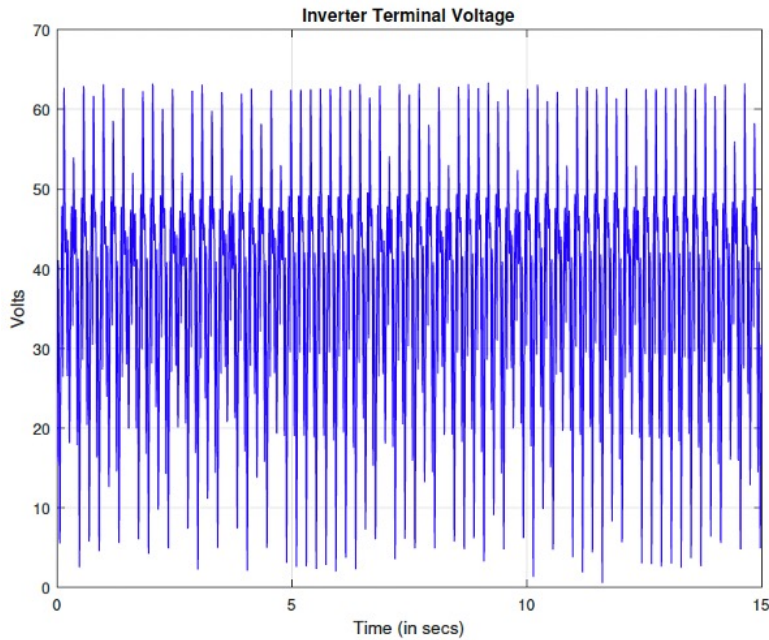
Case 4: ( $K_p = 5.5$ )  $\Rightarrow$  Period-4 Orbit ( $T=0.425s$ )



Bifurcation parameter is chosen as the proportional gain  $K_p$  of the current controller.

# GFL Inverter

Case 5: ( $K_p = 5.7$ )  $\Rightarrow$  Chaos

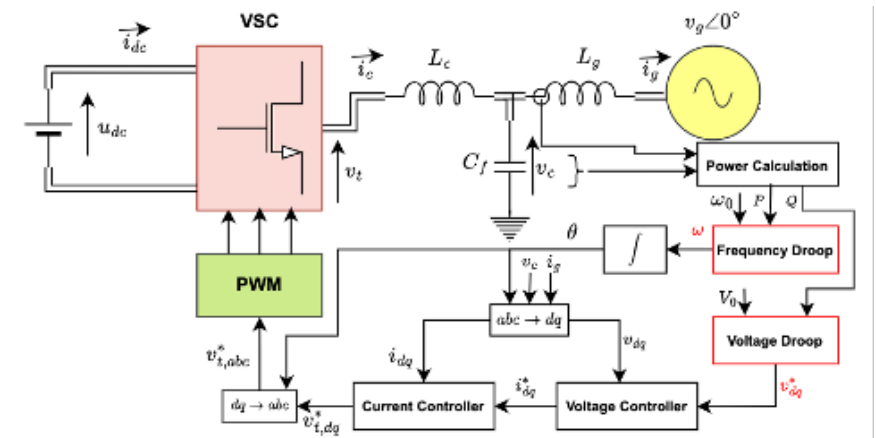
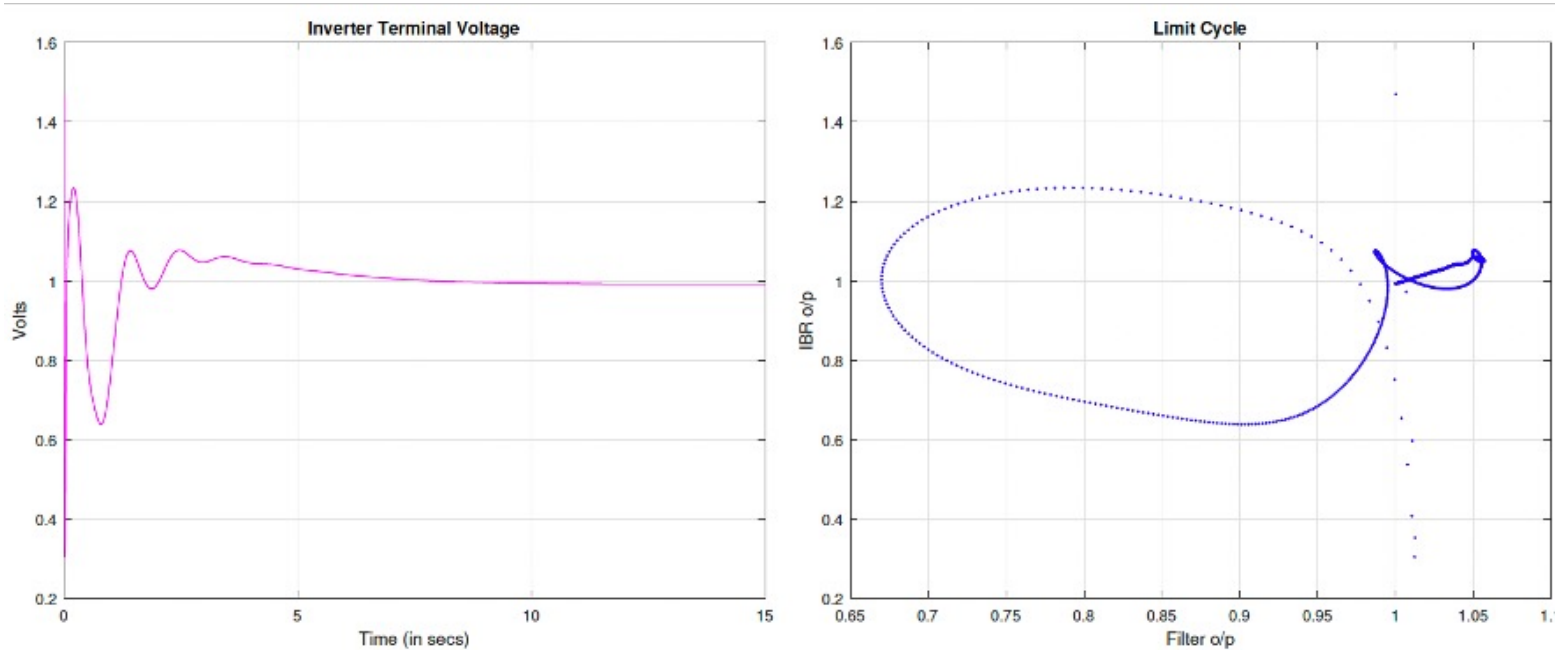


Bifurcation parameter is chosen as the proportional gain  $K_p$  of the current controller.



# GFM Inverter

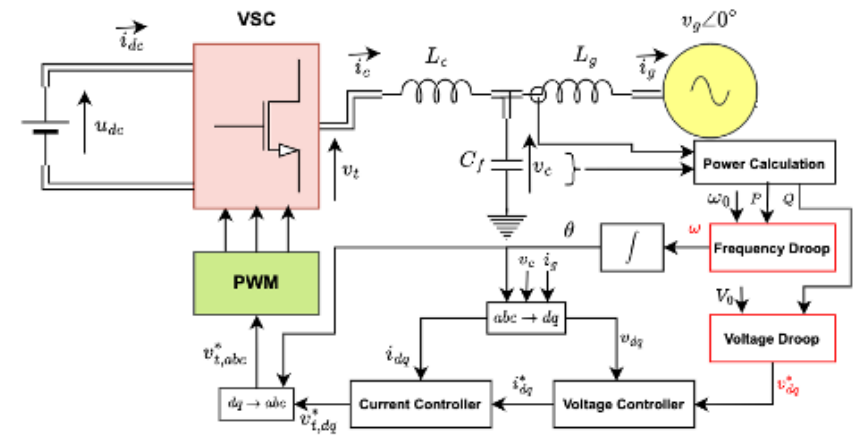
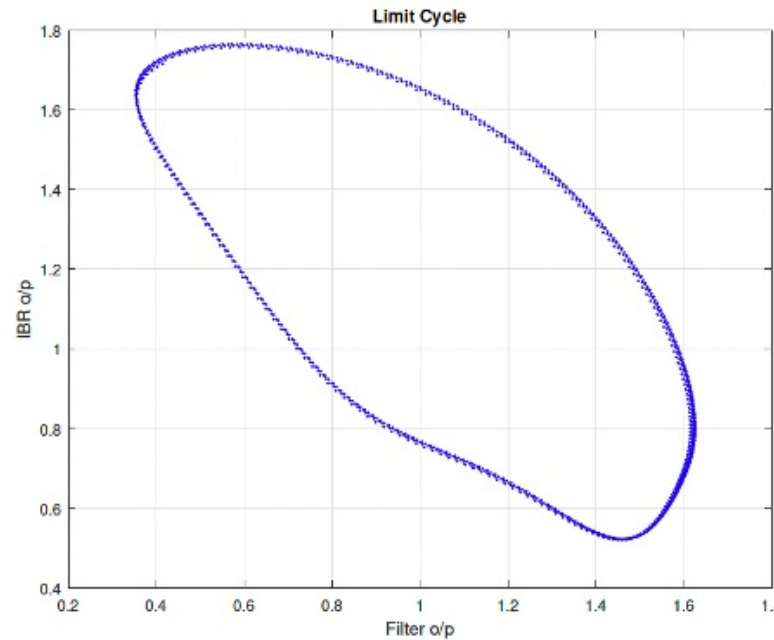
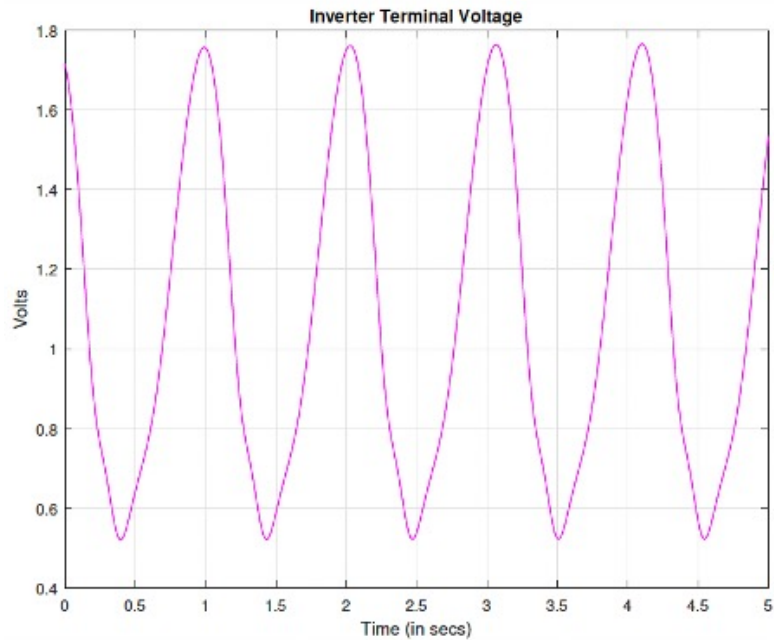
Case 1: Normal Operation ( $K_p = 2.5$ )  $\Rightarrow$  Fixed Point



Bifurcation parameter is chosen as the proportional gain  $K_p$  of the current controller.

# GFM Inverter

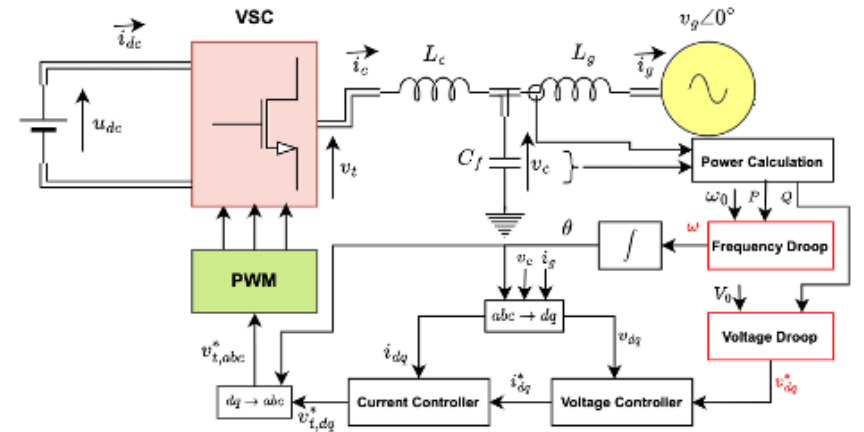
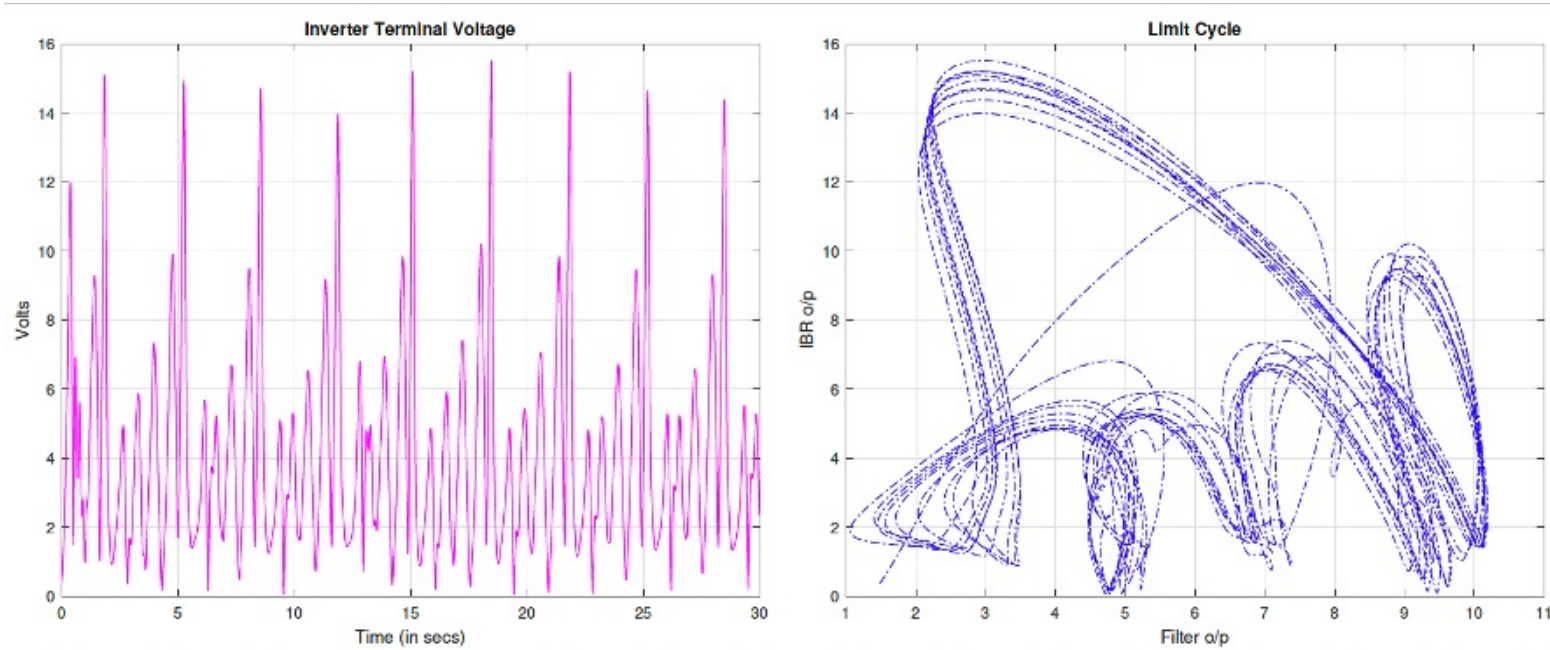
Case 2: ( $K_p = 0.636998540037319$ )  $\Rightarrow$  Period-1 Orbit



Bifurcation parameter is chosen as the proportional gain  $K_p$  of the current controller.

# GFM Inverter

Case 3: ( $K_p = 0.636998540037318$ )  $\Rightarrow$  Chaos



Bifurcation parameter is chosen as the proportional gain  $K_p$  of the current controller.



# Nonlinear Phenomena in IBR-rich Grids

1. Can IBR-rich power grids induce chaotic behavior?
2. Is there a fundamental difference between GFL and GFL Inverters?



## Observations:

- Grid-following (GFL) inverter  $\Rightarrow$  **Period-doubling** route
- Grid-forming (GFM) inverter  $\Rightarrow$  **Intermittency** route

**Observations:** GFM inverters can produce even more complex behavior

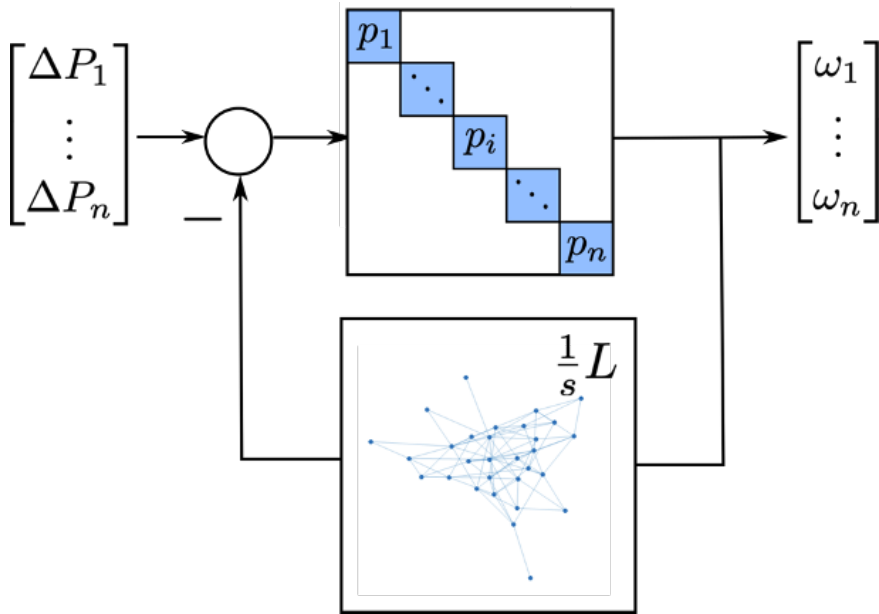
# Outline

- A Word of Caution: GFM IBRs Complex Dynamics
  - Faster controls **can speed up the transition to chaos**
- Decentralized Stability Analysis in Power Grids
  - Generalizing control tools for network systems
- Avenues for Future Research
  - Early detection via critical slow-down
  - Novel IBR control designs: Trading Freq. vs Volt. Support
  - The role of operations in SSO prevention

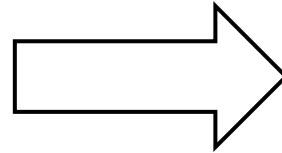
# Decentralized Stability Analysis in Power Grids [TCNS 19]



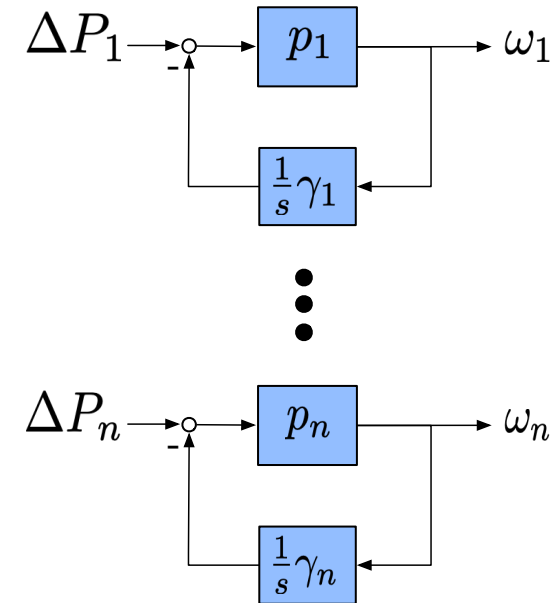
Richard Pates



1. When does this interconnection is stable?



2. Can we analysis and control design based on **local rules**?



## Problem Setup:

- *Linearized* power flows, *lossless*  

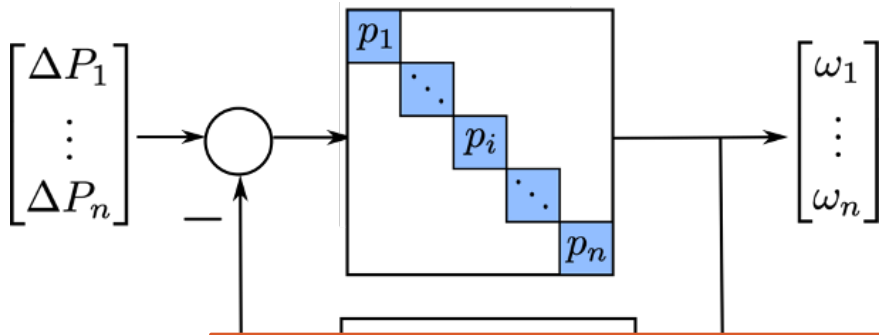
$$L_{ij} = b_{ij}v_i v_j \cos(\theta_i^* - \theta_j^*)$$
- Bus  $i$ : arbitrary *siso* transfer function:  

$$\omega_i = p_i(s) \Delta P_i \quad (\text{SGs or IBRs})$$

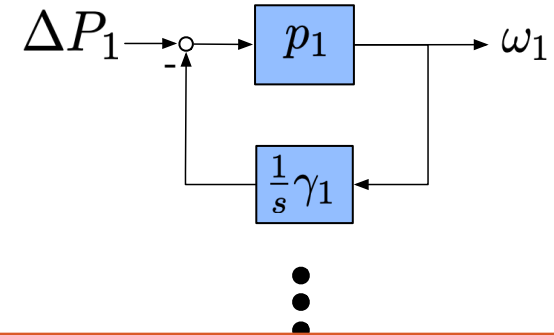
# Decentralized Stability Analysis in Power Grids [TCNS 19]



Richard Pates



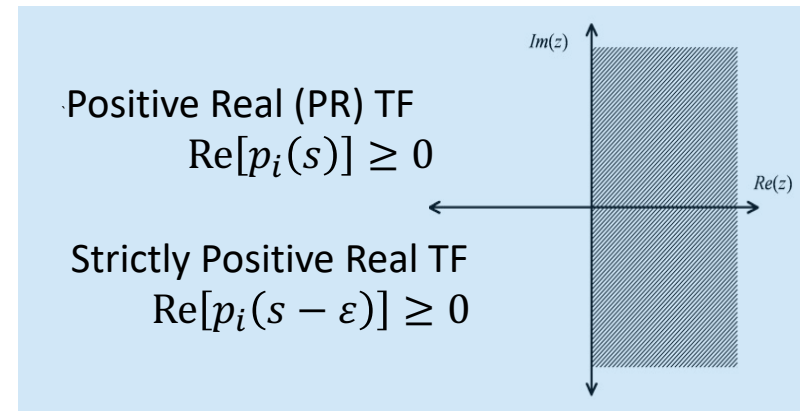
1. When does this interconnection is stable?



Can we use **network information** to relax passivity conditions?

## Standard Approach: Passivity

- If  $p_i(s)$  is strictly positive real (SPR), then the interconnection is stable for **all networks  $L$** !



# Classical Result: Absolute Stability

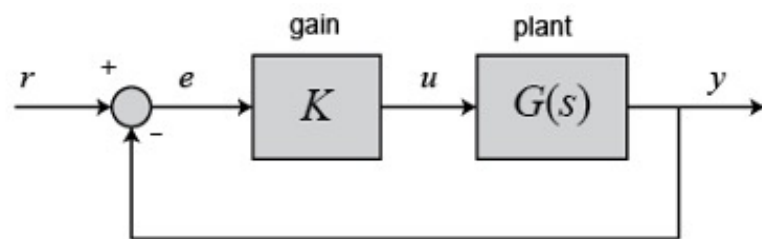
IEEE TRANSACTIONS ON AUTOMATIC CONTROL

## Frequency Domain Stability Criteria—Part I

R. W. BROCKETT, MEMBER, IEEE AND J. L. WILLEMS

Abstract—The objective of this paper is to illustrate the limita-

II. THE GENERALIZED POPOV THEOREM

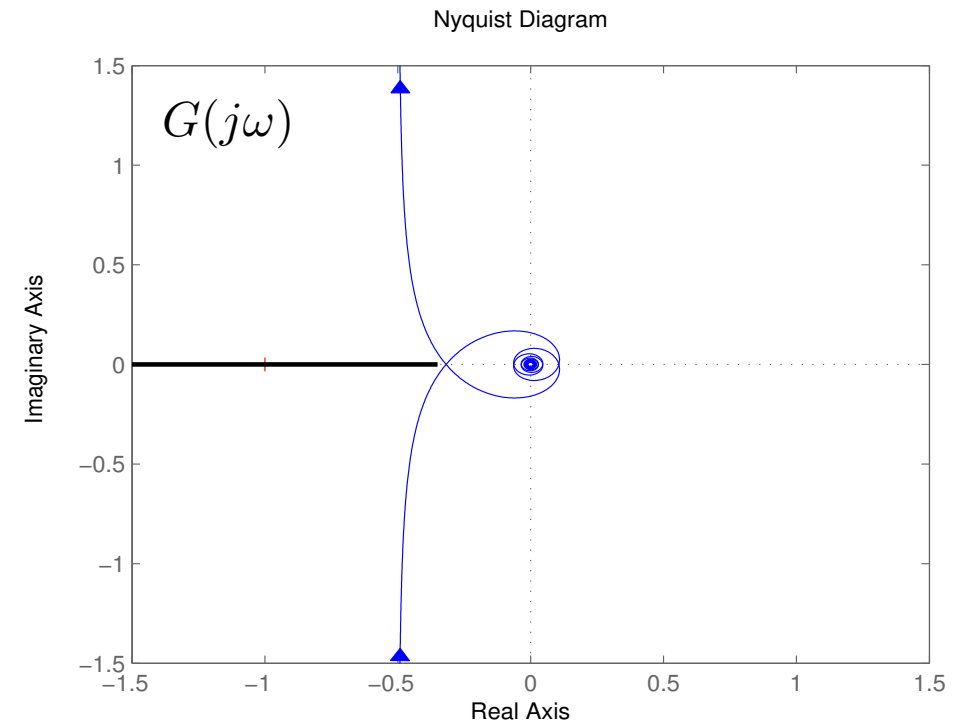


Stable for  $0 \leq K \leq k^*$ ?

**Assume:**  $G(s)$  is stable

**Define:**  $h(s) \in PR$  (passive)

**Test:** If  $h(s)(1 + k^*G(s)) \in SPR$  (strictly passive)  
then, **yes!**



# Classical Result: Absolute Stability

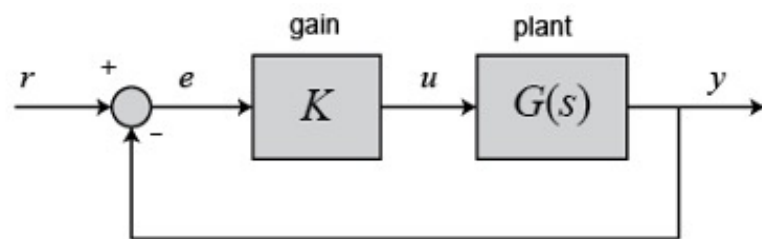
IEEE TRANSACTIONS ON AUTOMATIC CONTROL

## Frequency Domain Stability Criteria—Part I

R. W. BROCKETT, MEMBER, IEEE AND J. L. WILLEMS

Abstract—The objective of this paper is to illustrate the limita-

II. THE GENERALIZED POPOV THEOREM

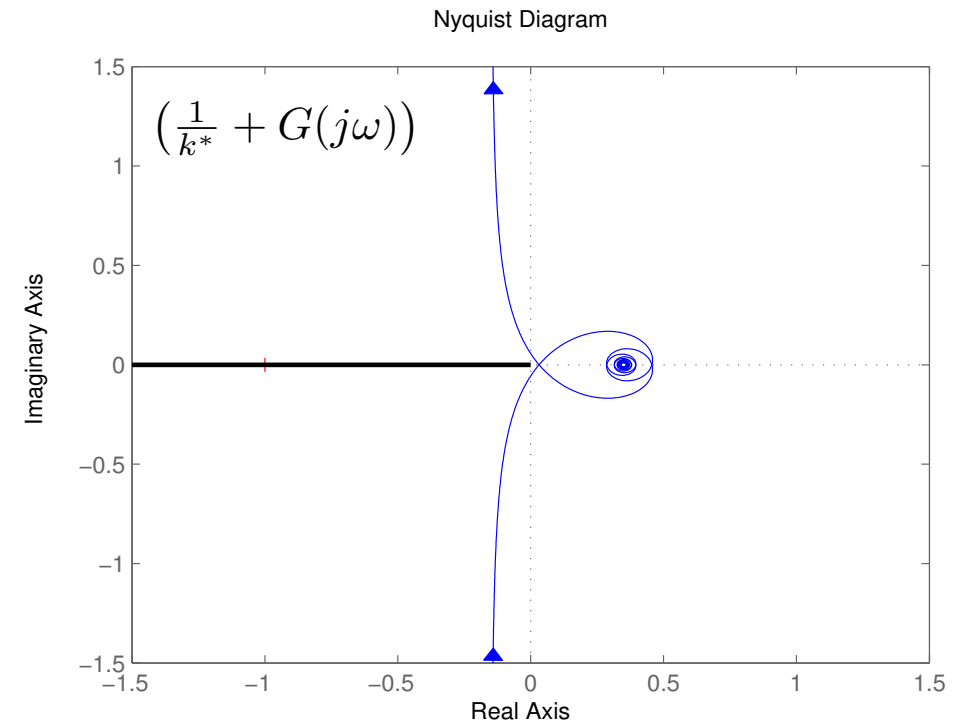


Stable for  $0 \leq K \leq k^*$ ?

**Assume:**  $G(s)$  is stable

**Define:**  $h(s) \in PR$  (passive)

**Test:** If  $h(s)(1 + k^*G(s)) \in SPR$  (strictly passive)  
then, **yes!**





# Classical Result: Absolute Stability

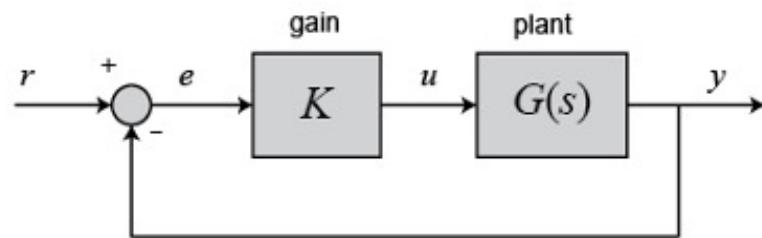
IEEE TRANSACTIONS ON AUTOMATIC CONTROL

## Frequency Domain Stability Criteria—Part I

R. W. BROCKETT, MEMBER, IEEE AND J. L. WILLEMS

Abstract—The objective of this paper is to illustrate the limita-

II. THE GENERALIZED POPOV THEOREM

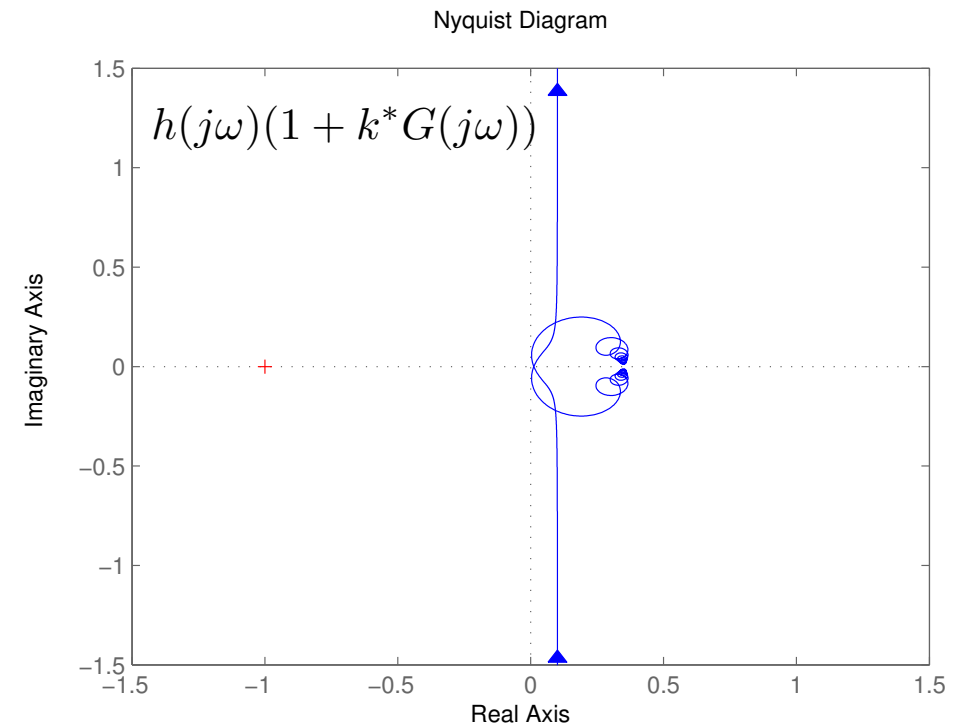


Stable for  $0 \leq K \leq k^*$ ?

**Assume:**  $G(s)$  is stable

**Define:**  $h(s) \in PR$  (passive)

**Test:** If  $h(s)(1 + k^*G(s)) \in SPR$  (strictly passive)  
then, **yes!**



# Scale-free Stability Analysis

**Key Idea:** Exploit limited network information to relax passivity condition

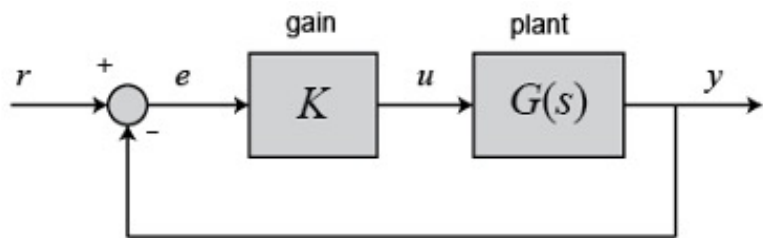
- Let  $\gamma_i$  be a local connectivity bound:  $[L]_{ii} = \sum_{j \in N_i} b_{ij} v_i v_j \cos(\theta_i^* - \theta_j^*) \leq \frac{\gamma_i}{2}$

**Brockett & Willems '65**

**Assume:**  $G(s)$  is stable

**Define:**  $h(s) \in PR$  (passive)

**Test:** If  $h(s)(1 + k^*G(s)) \in SPR$  (strictly) then system is stable for all  $0 \leq K \leq k^*$

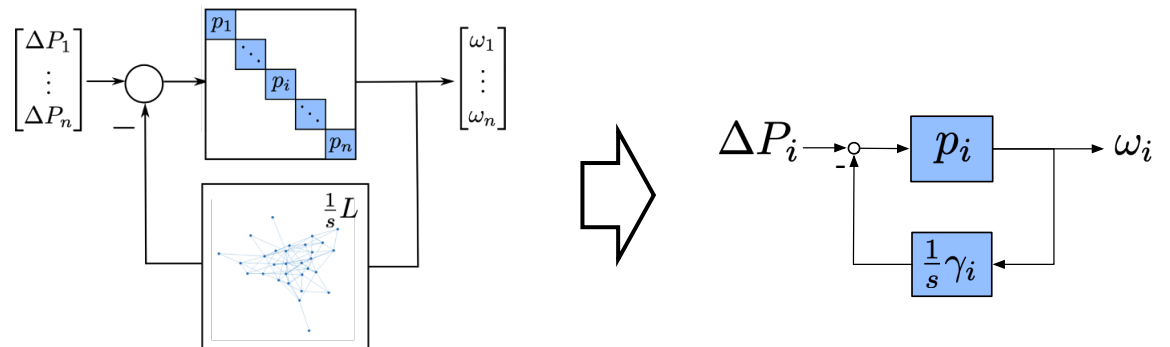


**Pates & Mallada 2019**

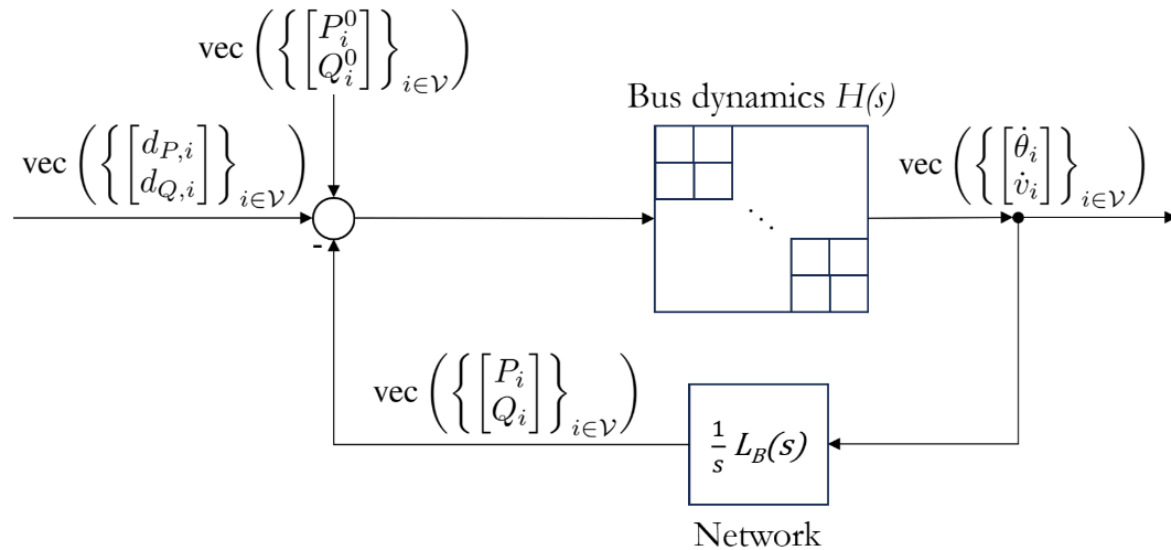
**Assume:**  $p_i(s)$  is stable

**Define:**  $h(s) \in PR$  (passive)

**Test:** If  $h(s) \left(1 + \gamma_i \frac{1}{s} p_i(s)\right) \in SPR, \forall i$ , then system stable for networks  $[L']_{ii} \leq \frac{\gamma_i}{2}, \forall i$



# Decentralized Stability Analysis for IBR Power Systems



## Bus dynamics: Droop-based grid-forming IBR (MIMO)

$$\begin{cases} \dot{\theta}_i &= \omega_i \\ \omega_i &= \omega_i^0 + m_i^p f_i^p(s)(P_i^0 - P_i), \\ v_i &= V_i^0 + m_i^q f_i^q(s)(Q_i^0 - Q_i). \end{cases} \quad \forall i \in \mathcal{V}_{inv}.$$

## Bus dynamics: Synchronous machine (SISO)

$$\dot{\theta}_i = \frac{1}{M_i s + D_i} P_i, \quad \forall i \in \mathcal{V}_{sm}.$$

### Theorem:

If for all  $i \in \mathcal{V}_{inv}$  the loop gain  $m_i^q$  satisfy

$$0 \leq m_i^q \leq \frac{1}{2(V_{\max,j} - V_{\min,i})|b_{ii}|}$$

for all  $j \in \mathcal{N}_i$ , then the system is stable

### Remarks:

- Fully decentralized (plug-and-play)
- Robust to network operating points
- Based on input-output models
- Several assumptions...

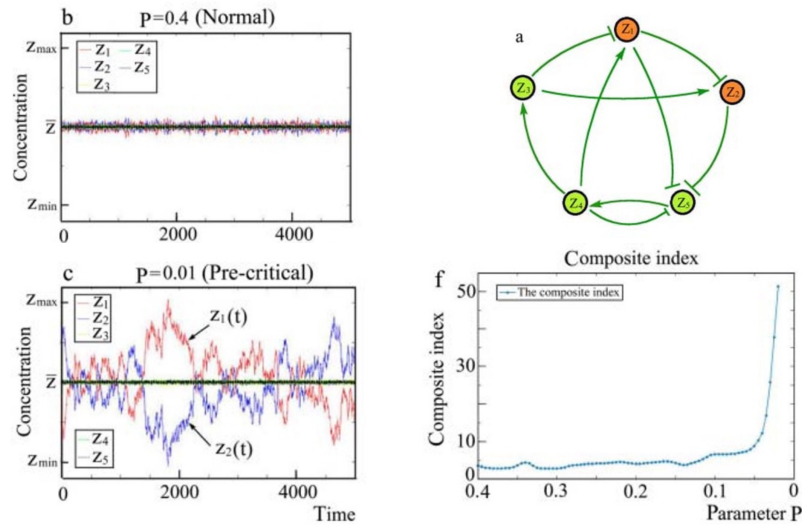
# Outline

- A Word of Caution: GFM IBRs Complex Dynamics
  - Faster controls **can speed up the transition to chaos**
- Scale-free Small-signal Stability Analysis
  - Generalizing control tools for network systems
- Avenues for Future Research
  - Early detection via critical slow-down
  - Novel IBR control designs: Trading Freq. vs Volt. Support
  - The role of operations in SSO prevention

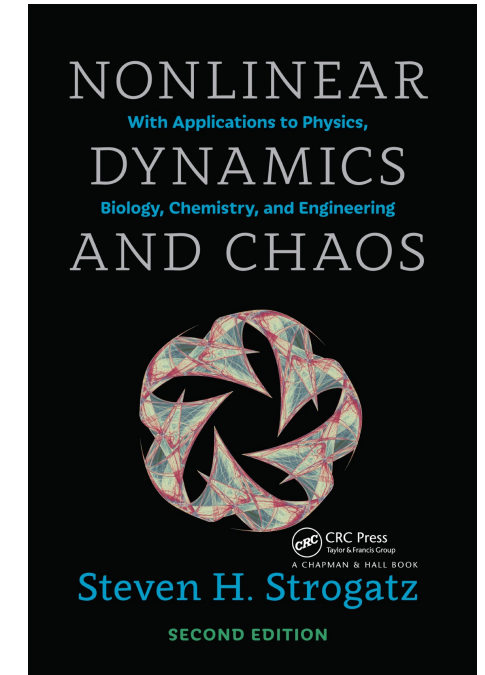
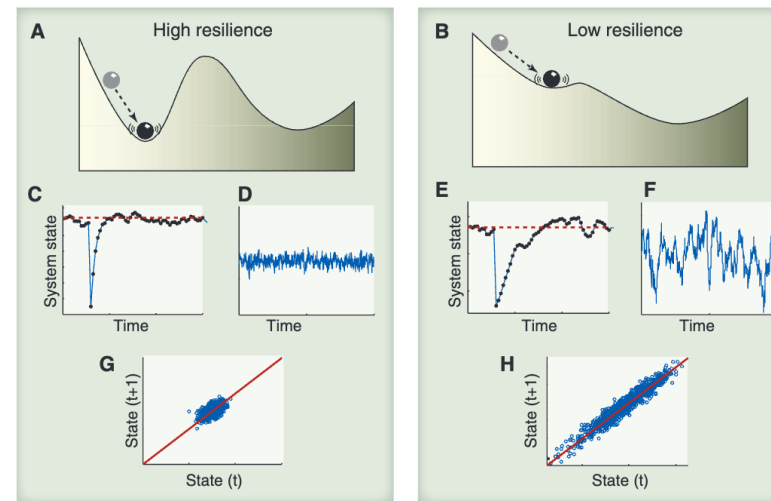
# Early Detection via Critical Slowdown

Transition to instability via bifurcations has the specific signature of *critical slowing down*

Early disease detection<sup>[1]</sup>



Loss of resilience<sup>[2]</sup>



## Research Questions:

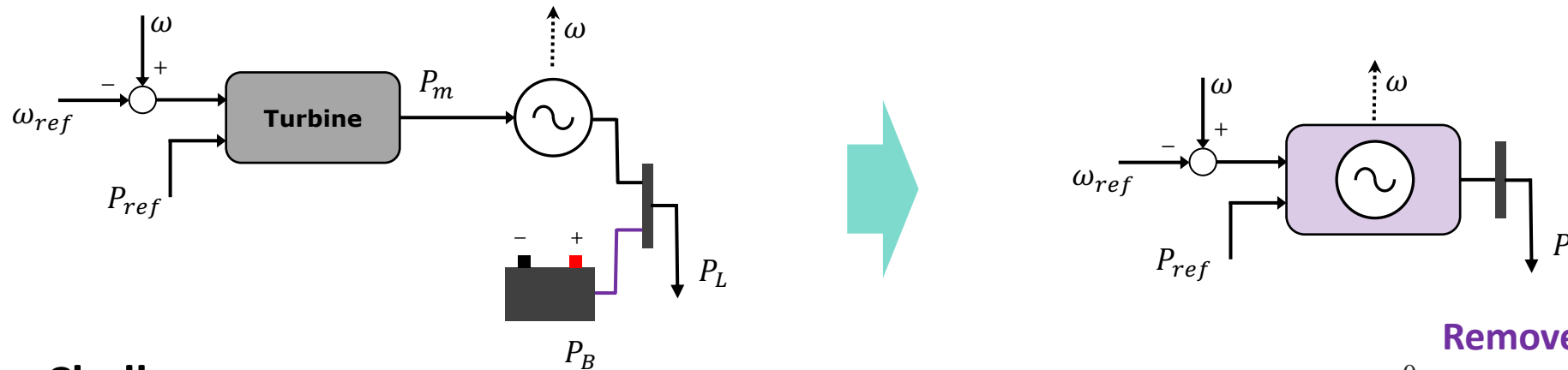
- Is critical slow-down a measurable feature in SSO transition to instability?
- Can we use critical slow down signatures to develop early alarm notifications?
  - What is the role of ML/AI in identifying these signatures?

[1] L. Chen et al. Detecting early-warning signals for sudden deterioration of complex diseases by dynamical network biomarkers, *Scientific reports* 2012

[2] M. Scheffer et al. Anticipating critical transitions, *Science* 2012

# Novel control designs for exploring trade-offs

IBR control flexibility enable control behavior not possible before: **Grid Shaping**



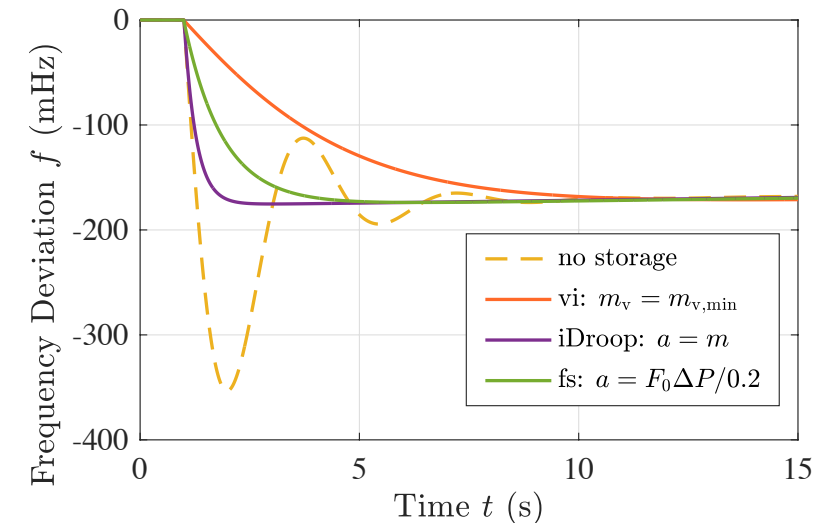
## Challenge:

- SSO limits inverter ability to shape frequency response

## Research Questions:

- Can we design controllers that trade-off between stability and performance?
- Can we dynamically tune controllers based on grid conditions?

Remove Nadir or Tuning RoCoF



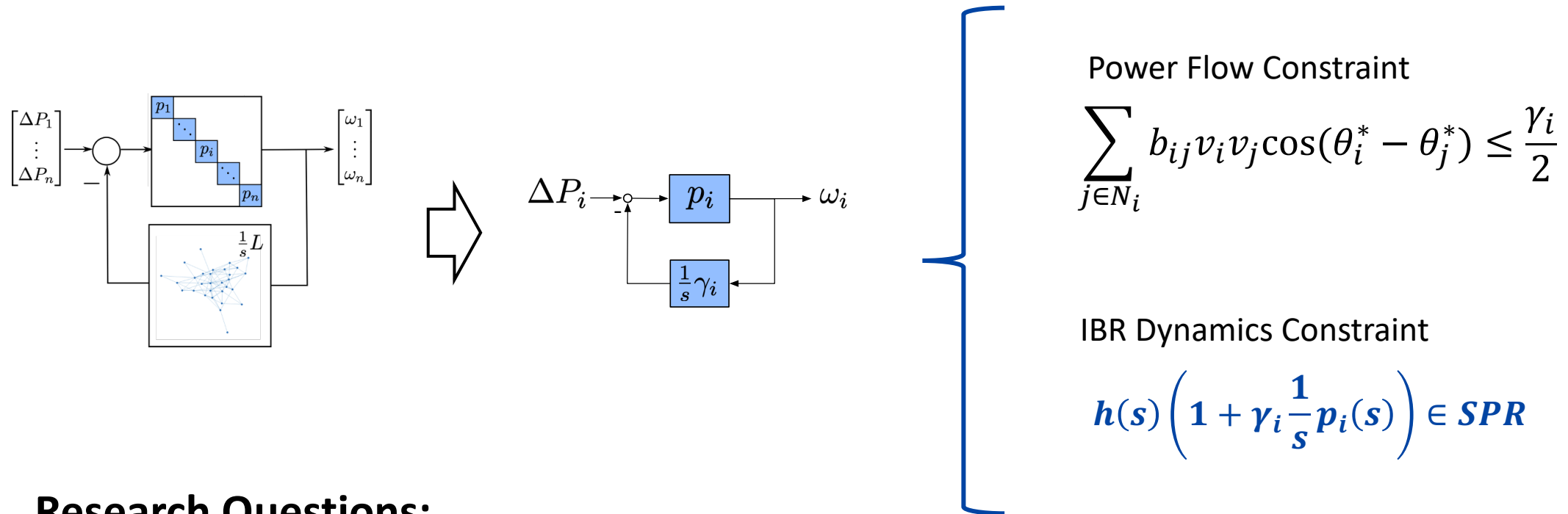
[LCSS 20] Jiang, Bernstein, Vorobev, M. Grid-forming frequency shaping control for low-inertia power systems **IEEE Control Systems Letters** 2020

[LCSS 23] Poolla, Lin, Bernstein, M, Groß. Frequency shaping control for weakly-coupled grid-forming IBRs **IEEE Control Systems Letters** 2023



# The role of Operations in SSO prevention

Emergence of oscillations depends on *grid conditions* and *control tuning*



## Research Questions:

- Can we design dispatch mechanisms that can prevent SSO?
- Can dispatch mechanisms also inform about control tuning?
- How should we implement such mechanisms with inaccurate models?

# Summary

- A Word of Caution: GFM IBRs Complex Dynamics
  - Faster controls **can speed up the transition to chaos**
- Scale-free Small-signal Stability Analysis
  - Generalizing control tools for network systems
- Avenues for Future Research
  - Early detection via critical slow-down
  - Novel IBR control designs: Trading Freq. vs Volt. Support
  - The role of operations in SSO prevention

# Thanks!