

Grid Shaping Control for High-IBR Power Systems

Stability Analysis and Control Design

Enrique Mallada



GE EDGE Symposium

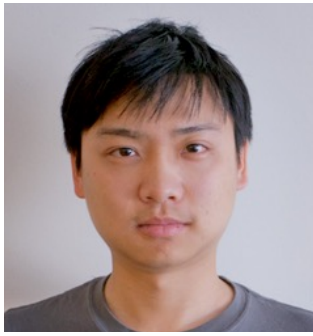
September 20, 2023

Acknowledgements

Students



Yan Jiang



Hancheng Min



Eliza Cohn



Collaborators



Petr Vorobev



Richard Pates



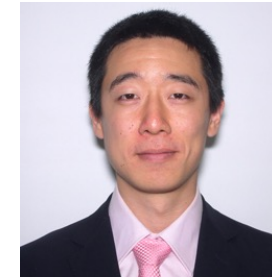
Fernando Paganini



Dominic Groß



Bala K. Poolla

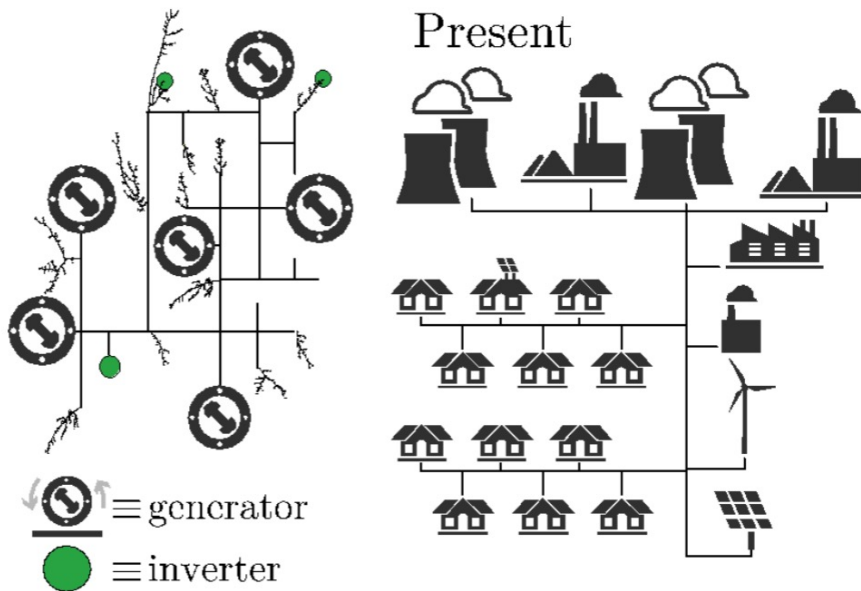


Yashen Lin



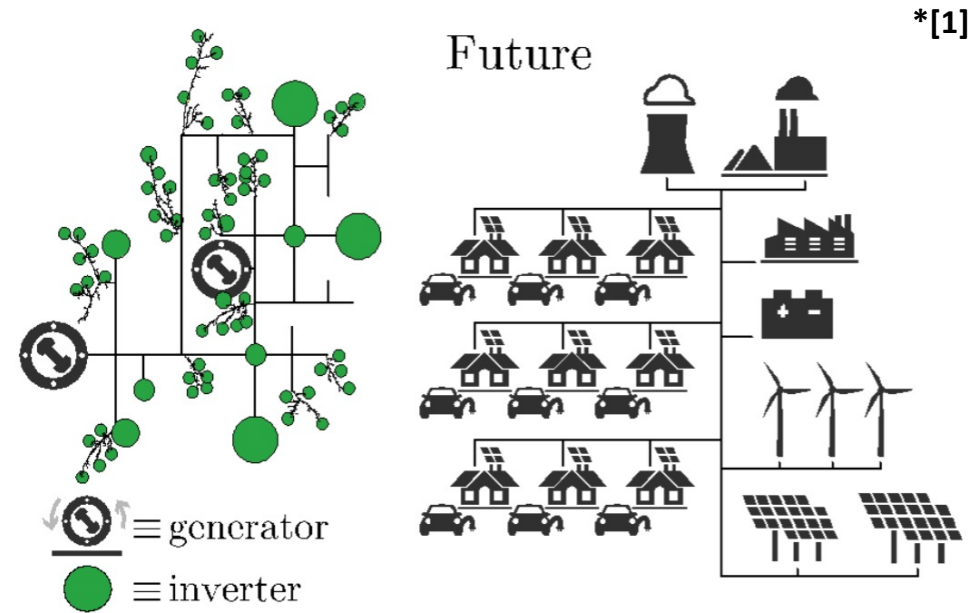
Andrey Bernstein

The Future Grid



Present grid

- dispatchable generation
- high inertial response
- strong voltage support
- well known physics

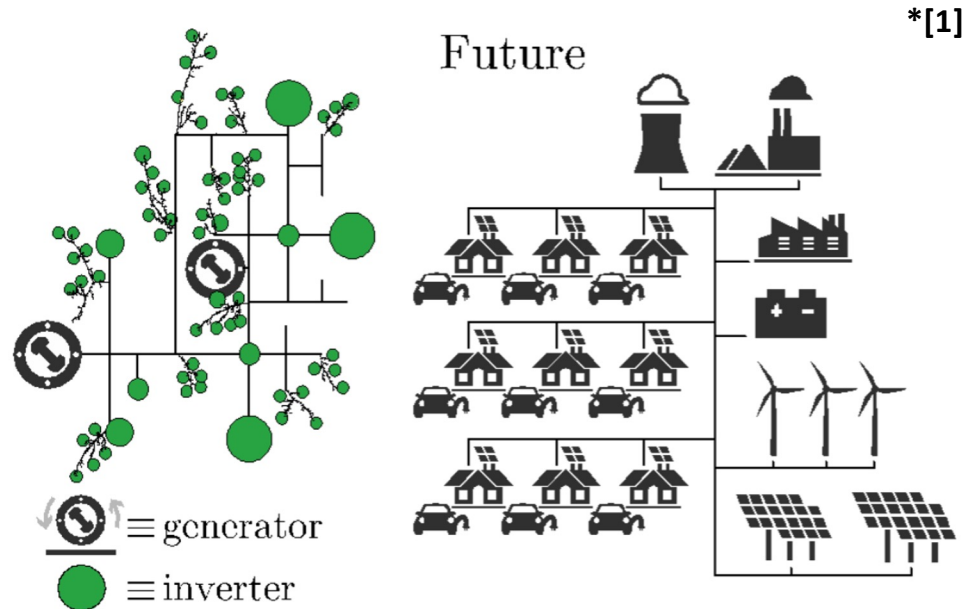


Future

- variable and distributed generation
- limited inertia levels
- weak voltage support
- proprietary control laws (black box)

[1] Lin et al. Research roadmap on grid-forming inverters. Technical report, National Renewable Energy Lab.(NREL), Golden CO, 2020

The Future Grid



Future

- variable and distributed generation
- limited inertia levels
- weak voltage support
- proprietary control laws (black box)

Selected challenges

- increased system **uncertainty**
- **sensitivity** to disturbances
- new forms of **instabilities**, induced by inverter-based resources
- need to compensate for **reduced inertia**

Research questions:

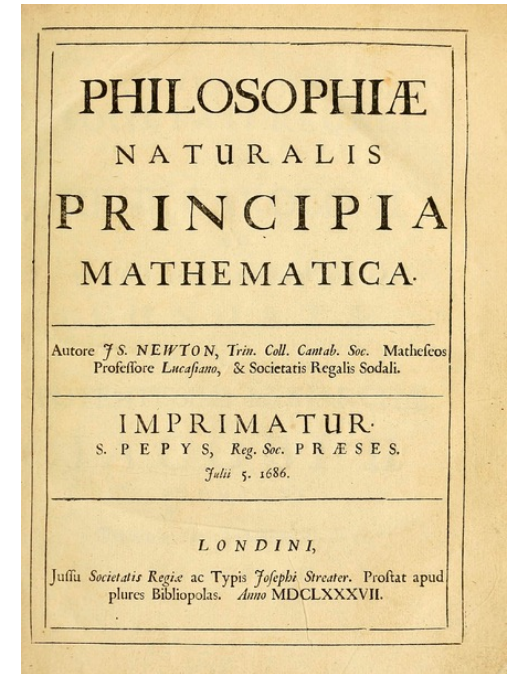
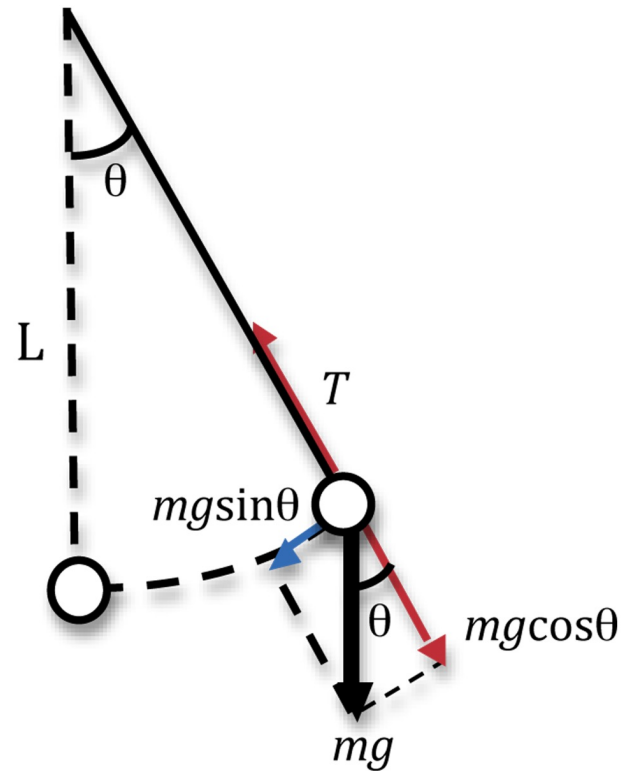
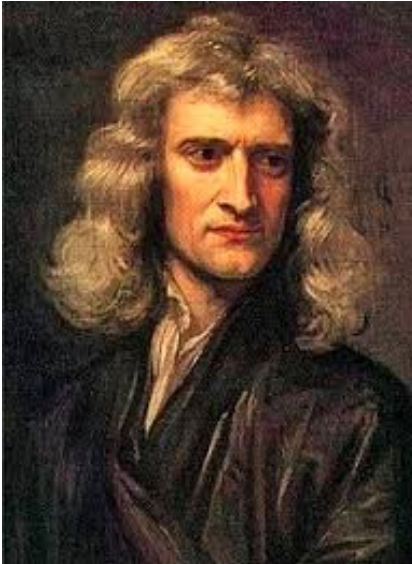
- How should we control a grid with limited inertial/voltage support?
- Should we try to mimic SGs response? Or find new and more efficient control paradigms, suitable for IBRs?

[1] Lin et al. Research roadmap on grid-forming inverters. Technical report, National Renewable Energy Lab.(NREL), Golden CO, 2020

Outline

- Merits and trade-offs of low inertia
 - Control Perspective: Lighter systems are easier to control!
- Scale-free Stability Analysis of Grids
 - Generalizes passivity notions using network information
- Grid Shaping Control
 - Grid-following/forming control framework for controlling future grids

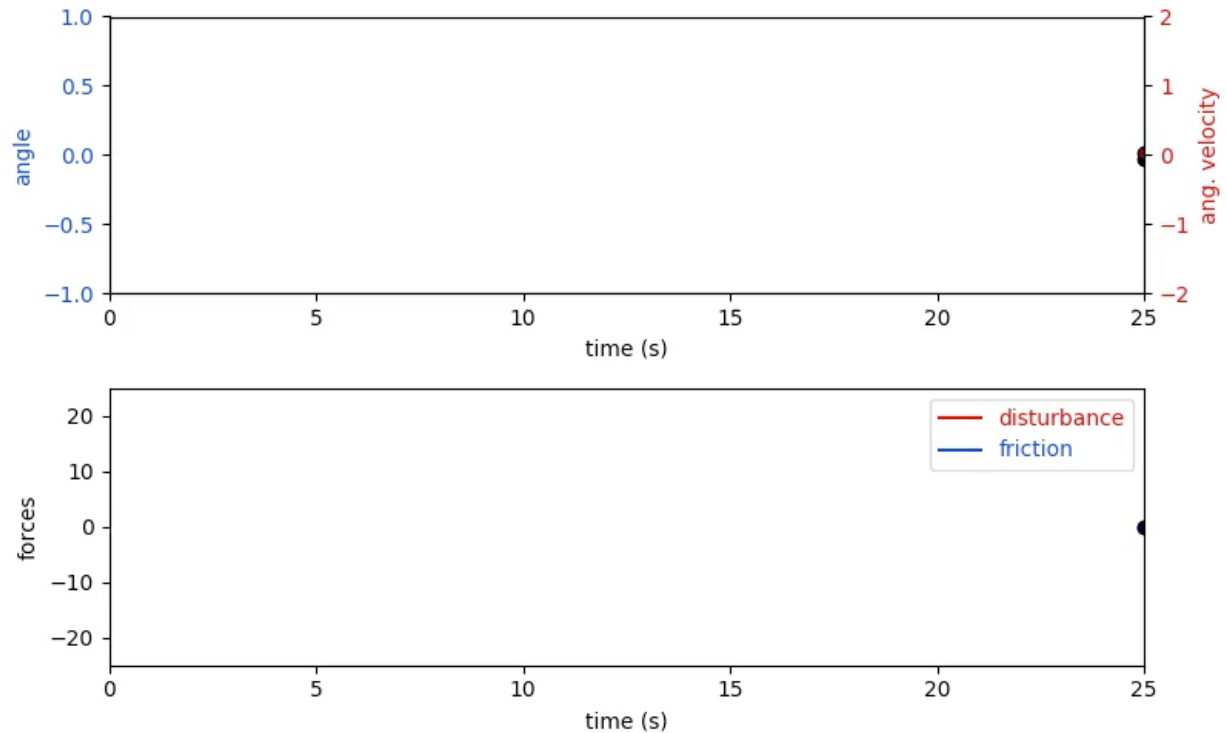
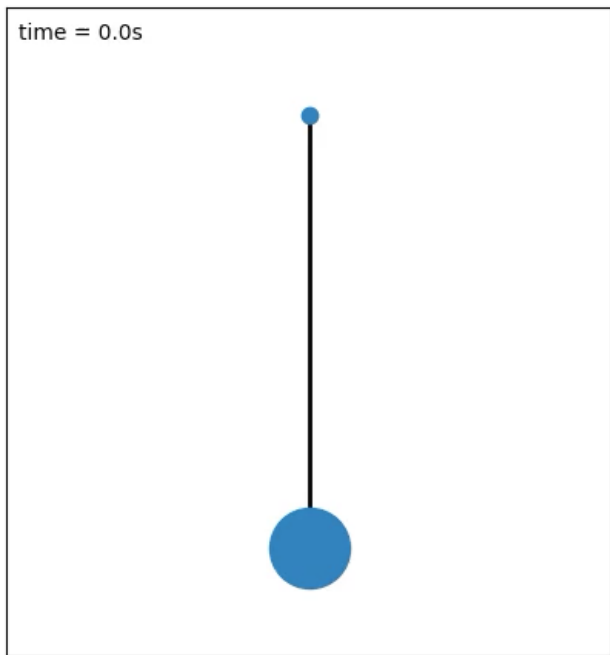
Merits and Tradeoffs of Inertia



$$\ddot{\theta} = -\frac{d}{m}\dot{\theta} - g \sin \theta + \frac{f}{m}$$

Merits and Trade-offs of Inertia

$$\ddot{\theta} = -\frac{d}{m}\dot{\theta} - g \sin \theta + \frac{f}{m}$$

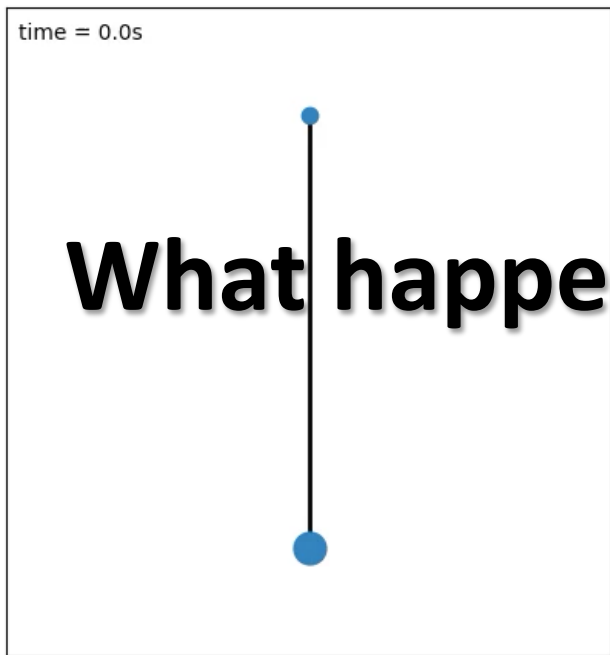


Pros: Provides natural disturbance rejection

Cons: Hard to regain steady-state

Merits and Trade-offs of **Low** Inertia

$$\ddot{\theta} = -\frac{d}{m}\dot{\theta} - g \sin \theta + \frac{f}{m}$$



What happens when one adds **control**?

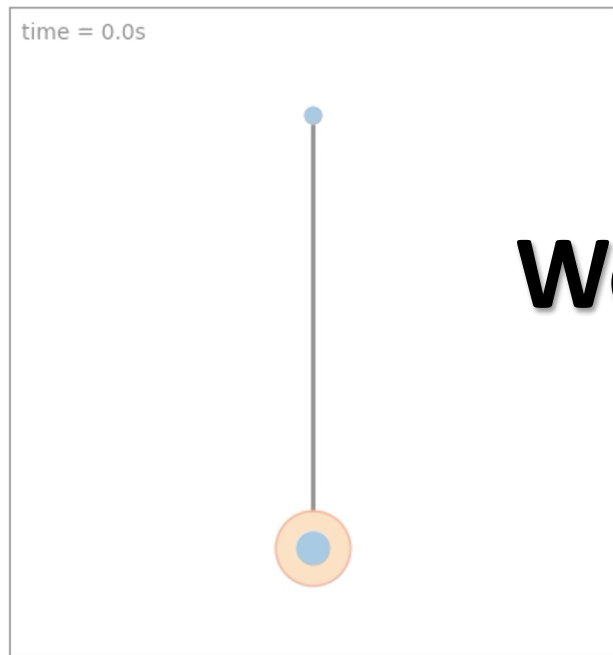


Cons: Susceptible to disturbances

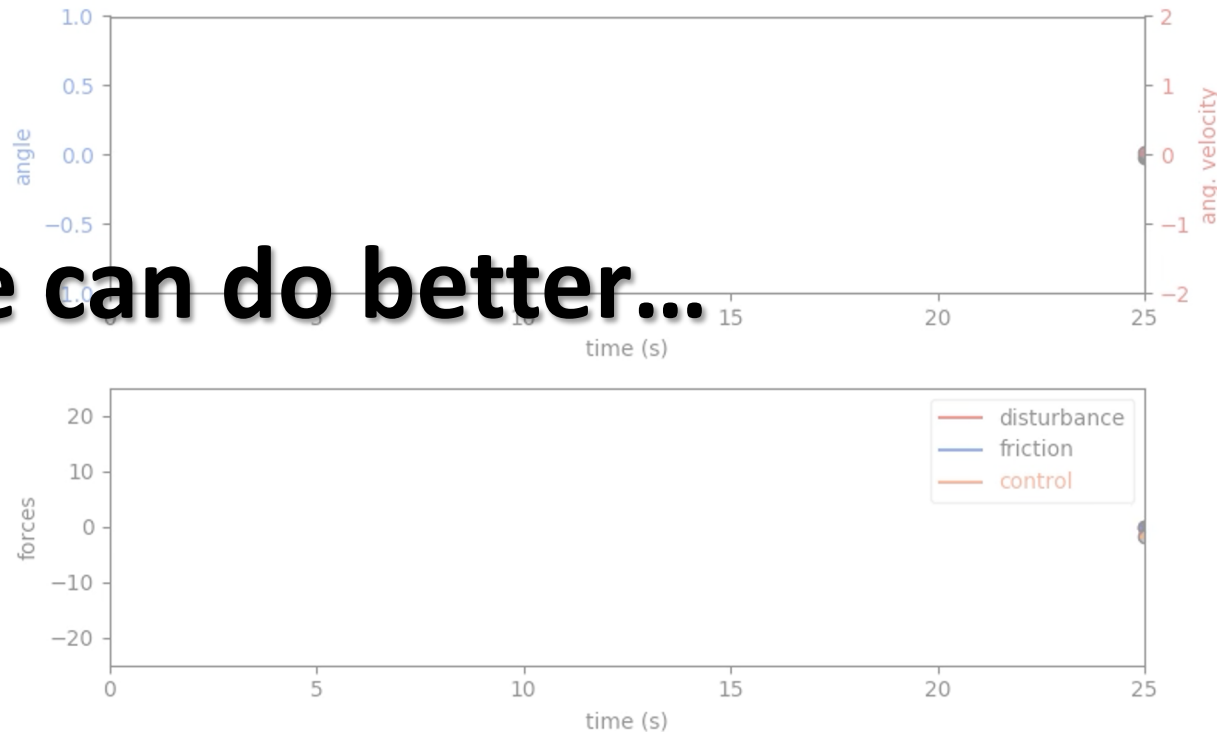
Pros: Regains steady-state faster

Control of **Low** Inertia Pendulum

Virtual **Mass** Control: $m\ddot{\theta} = -d\dot{\theta} - mg \sin \theta + f - \nu\ddot{\theta}$



We can do better...



Pros:

Provides disturbance rejection

Cons:

Hard to regain steady-state + **excessive control effort**

Control of **Low** Inertia Pendulum



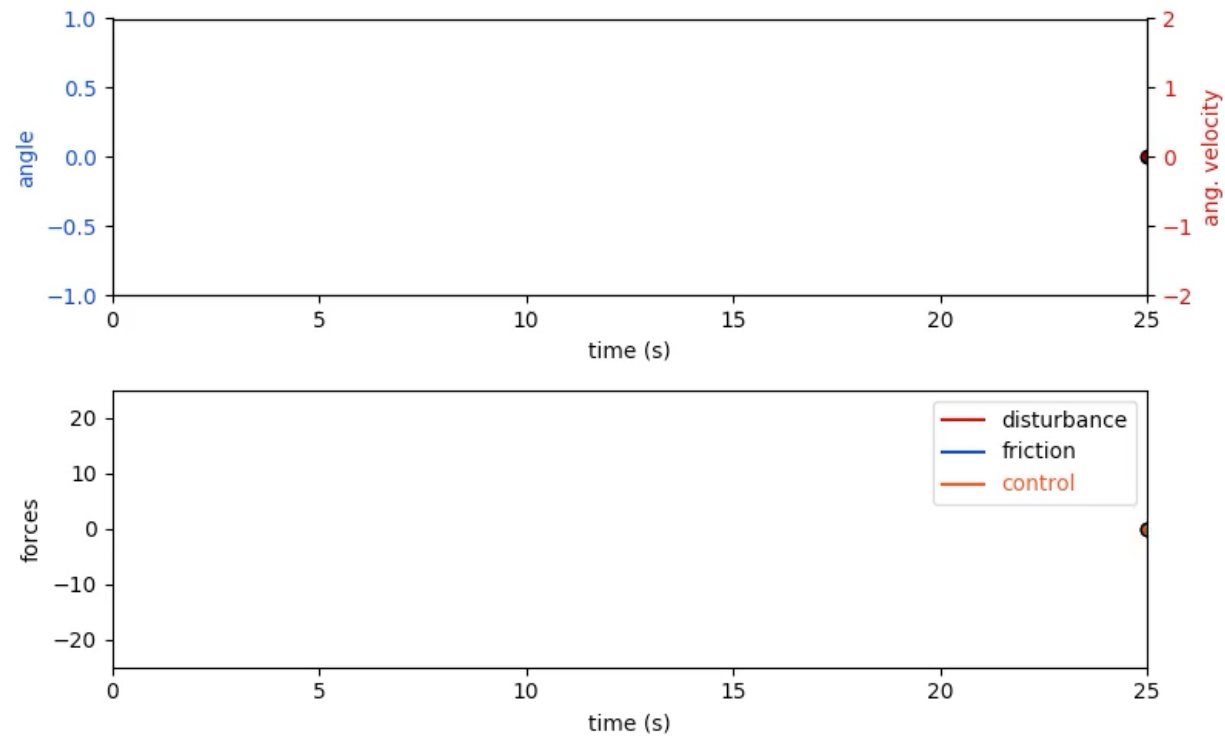
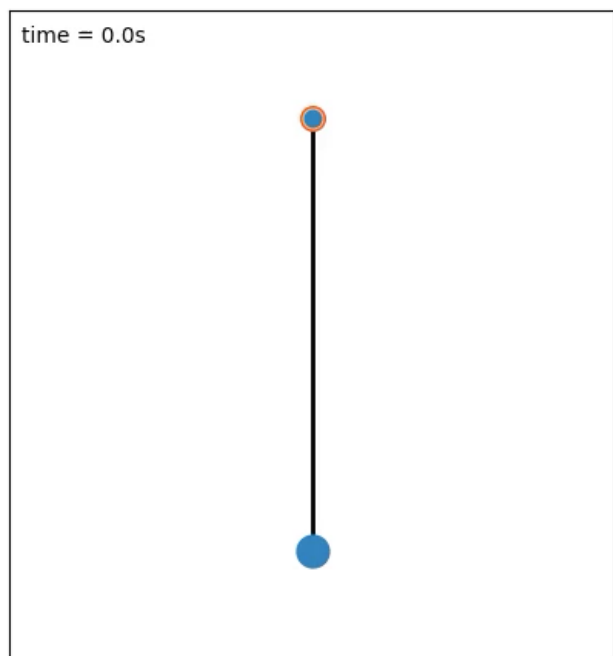
Yan Jiang



Richard Pates

Dynamic Droop:

$$m\ddot{\theta} = -d\dot{\theta} - mg \sin \theta + f + x$$
$$\tau' \dot{x} = -x - (r_r^{-1} \dot{\theta} + \tau' \nu' \ddot{\theta})$$



Control of **Low** Inertia Pendulum

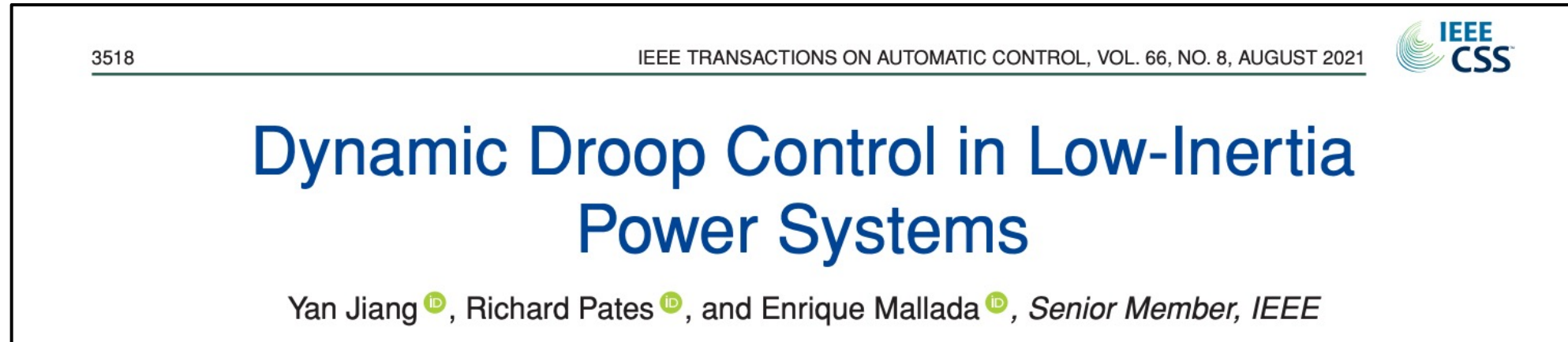


Yan Jiang



Richard Pates

Dynamic Droop: $m\ddot{\theta} = -d\dot{\theta} - mg \sin \theta + f + x$



Dynamic Droop Benefits

- Overshoot Elimination in Nadir
- Disturbance Rejection
- Noise Attenuation
- Reduce Inter-area Oscillations

Caveat

- Control design limited to co-located resources (SGs and IBRs)

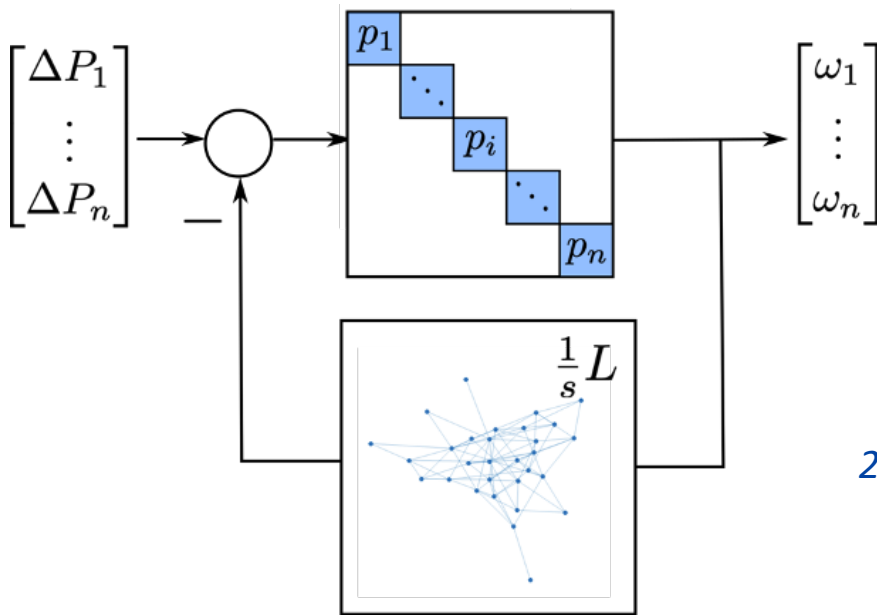
Outline

- Merits and trade-offs of low inertia
 - Control Perspective: Lighter systems are easier to control!
- Scale-free Stability Analysis of Grids
 - Generalizes passivity notions using network information
- Grid Shaping Control
 - Grid-following/forming control framework for controlling future grids

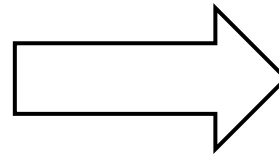
Decentralized Stability Analysis in Power Grids [TCNS 19]



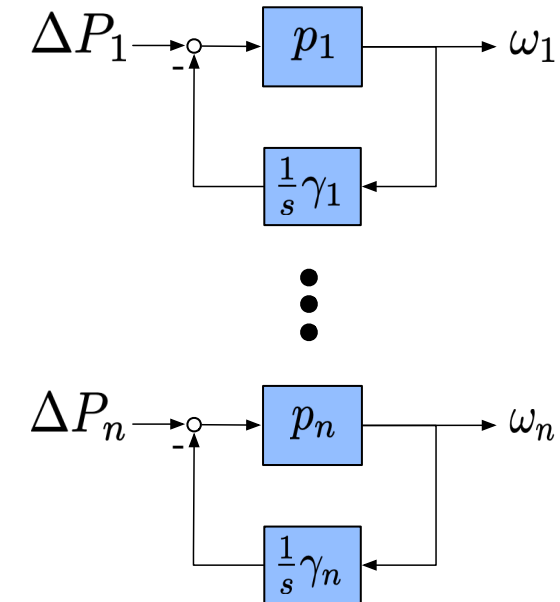
Richard Pates



1. When does this interconnection is stable?



2. Can we do analysis and control design based on **local** rules?



Problem Setup:

- Linearized power flows, lossless

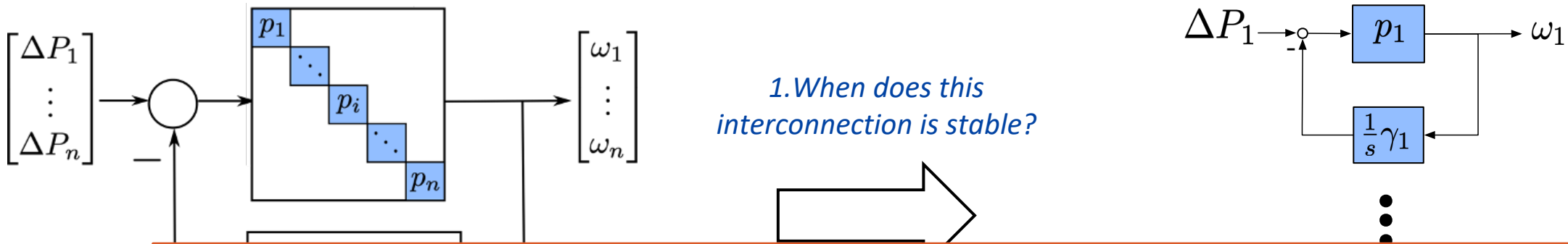
$$L_{ij} = b_{ij}v_i v_j \cos(\theta_i^* - \theta_j^*)$$
- Bus i : arbitrary siso transfer function:

$$\omega_i = p_i(s) \Delta P_i \quad (\text{SGs or IBRs})$$

Decentralized Stability Analysis in Power Grids [TCNS 19]



Richard Pates



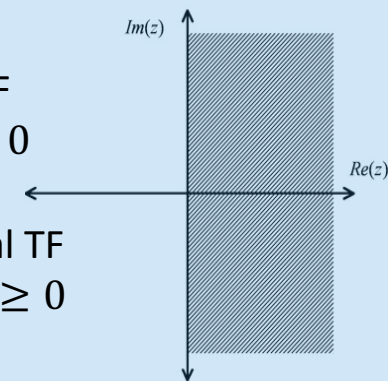
Can we use **network information** to relax passivity conditions?

Standard Approach: Passivity

- If $p_i(s)$ is strictly positive real (SPR), then the interconnection is stable for **all networks L** !

Positive Real (PR) TF
 $\text{Re}[p_i(s)] \geq 0$

Strictly Positive Real TF
 $\text{Re}[p_i(s - \varepsilon)] \geq 0$



Classical Result: Absolute Stability

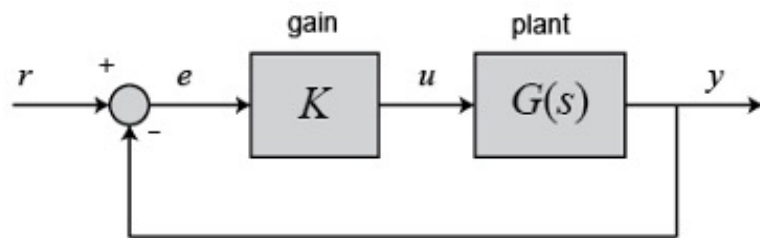
IEEE TRANSACTIONS ON AUTOMATIC CONTROL

Frequency Domain Stability Criteria—Part I

R. W. BROCKETT, MEMBER, IEEE AND J. L. WILLEMS

Abstract—The objective of this paper is to illustrate the limita-

II. THE GENERALIZED POPOV THEOREM

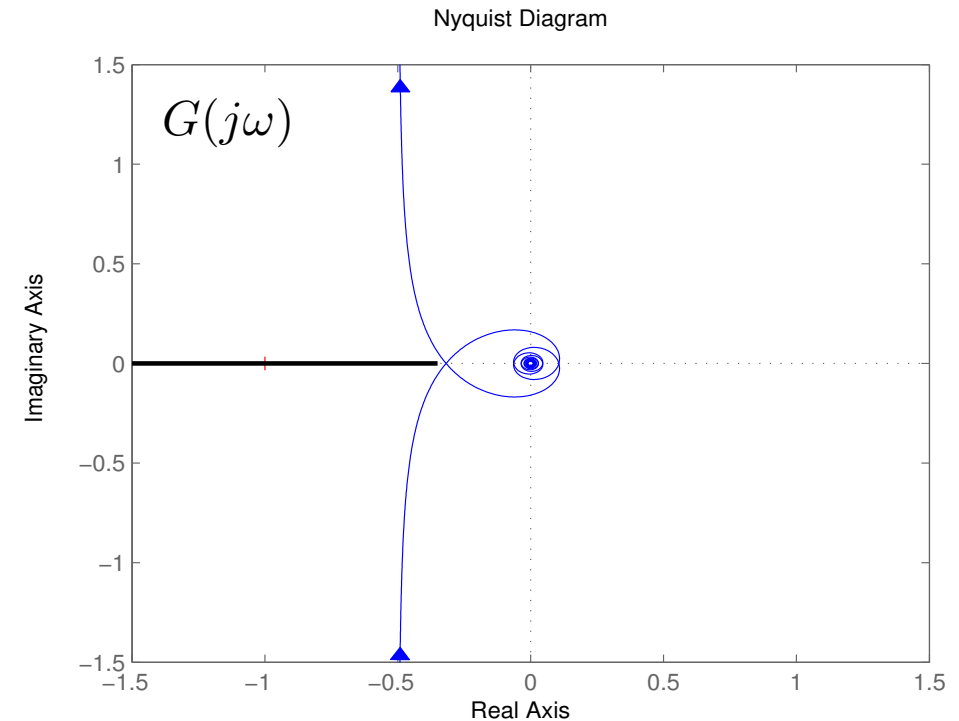


Stable for $0 \leq K \leq k^*$?

Assume: $G(s)$ is stable

Define: $h(s) \in PR$ (passive)

Test: If $h(s)(1 + k^*G(s)) \in SPR$ (strictly passive)
then, **yes!**



Classical Result: Absolute Stability

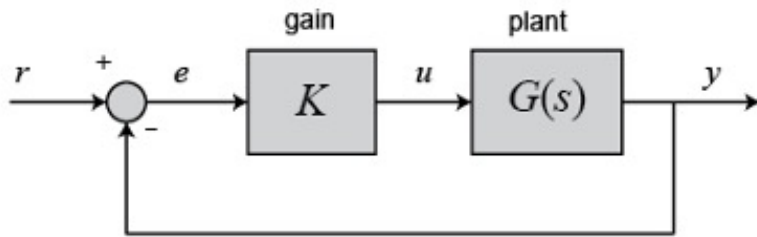
IEEE TRANSACTIONS ON AUTOMATIC CONTROL

Frequency Domain Stability Criteria—Part I

R. W. BROCKETT, MEMBER, IEEE AND J. L. WILLEMS

Abstract—The objective of this paper is to illustrate the limita-

II. THE GENERALIZED POPOV THEOREM

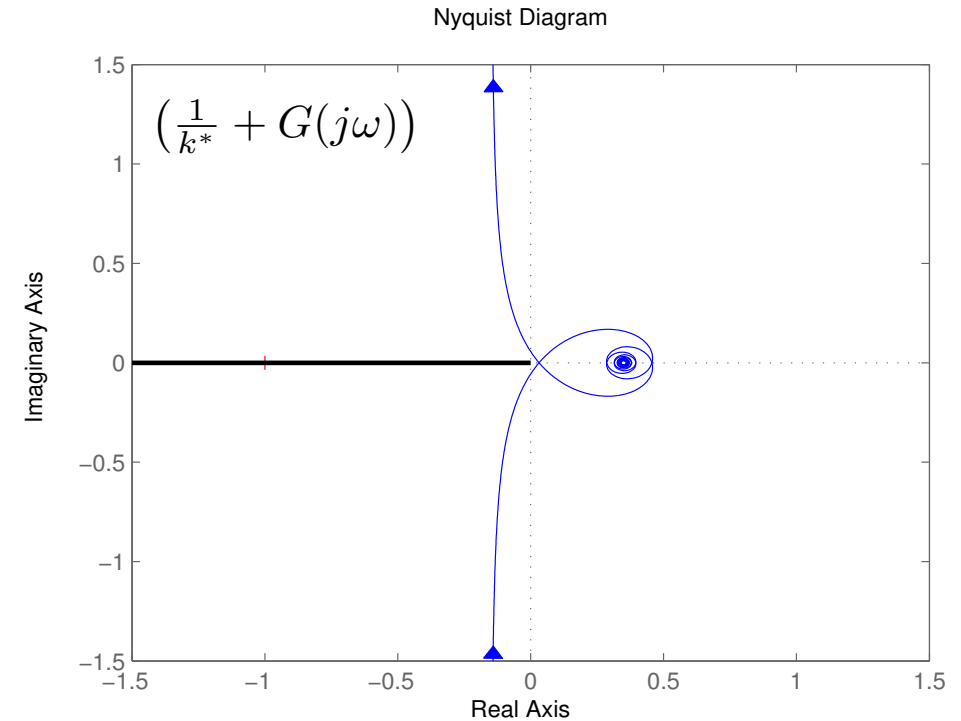


Stable for $0 \leq K \leq k^*$?

Assume: $G(s)$ is stable

Define: $h(s) \in PR$ (passive)

Test: If $h(s)(1 + k^*G(s)) \in SPR$ (strictly passive)
then, **yes!**



Classical Result: Absolute Stability

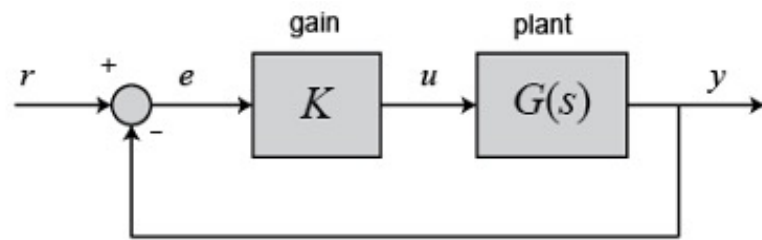
IEEE TRANSACTIONS ON AUTOMATIC CONTROL

Frequency Domain Stability Criteria—Part I

R. W. BROCKETT, MEMBER, IEEE AND J. L. WILLEMS

Abstract—The objective of this paper is to illustrate the limita-

II. THE GENERALIZED POPOV THEOREM

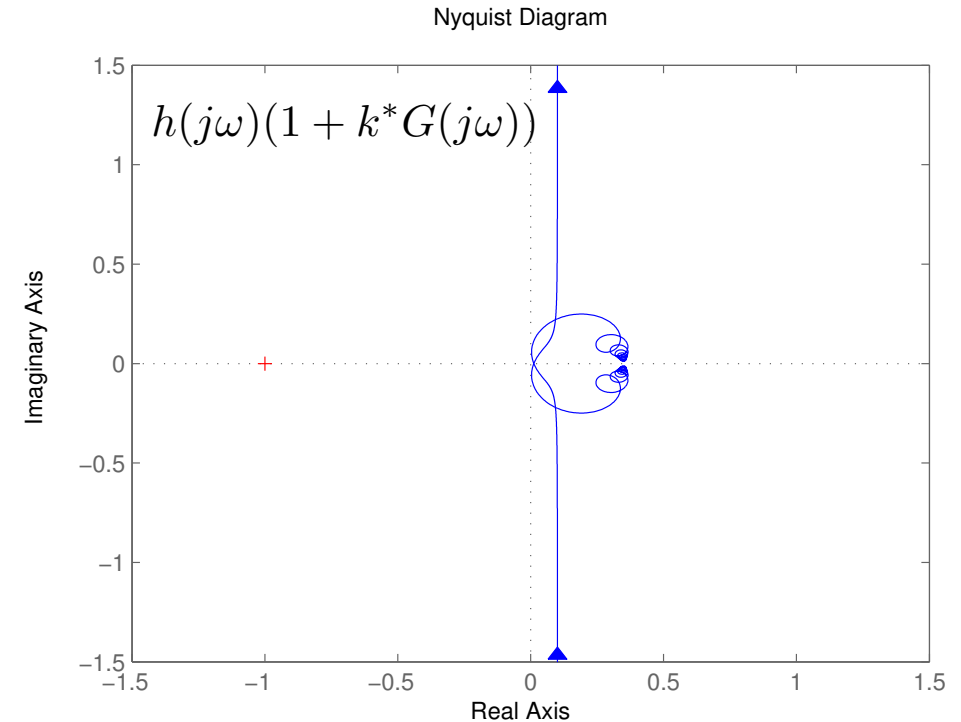


Stable for $0 \leq K \leq k^*$?

Assume: $G(s)$ is stable

Define: $h(s) \in PR$ (passive)

Test: If $h(s)(1 + k^*G(s)) \in SPR$ (strictly passive)
then, **yes!**



Scale-free Stability Analysis

Key Idea: Exploit limited network information to relax passivity condition

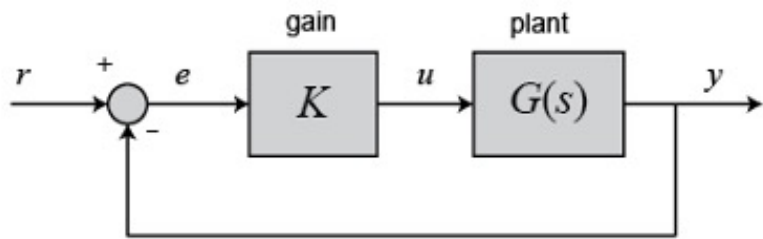
- Let γ_i be a local connectivity bound: $[L]_{ii} = \sum_{j \in N_i} L_{ij} \leq \frac{\gamma_i}{2}$

Brockett & Willems '65

Assume: $G(s)$ is stable

Define: $h(s) \in PR$ (passive)

Test: If $h(s)(1 + k^*G(s)) \in SPR$ (strictly) then system is stable for all $0 \leq K \leq k^*$

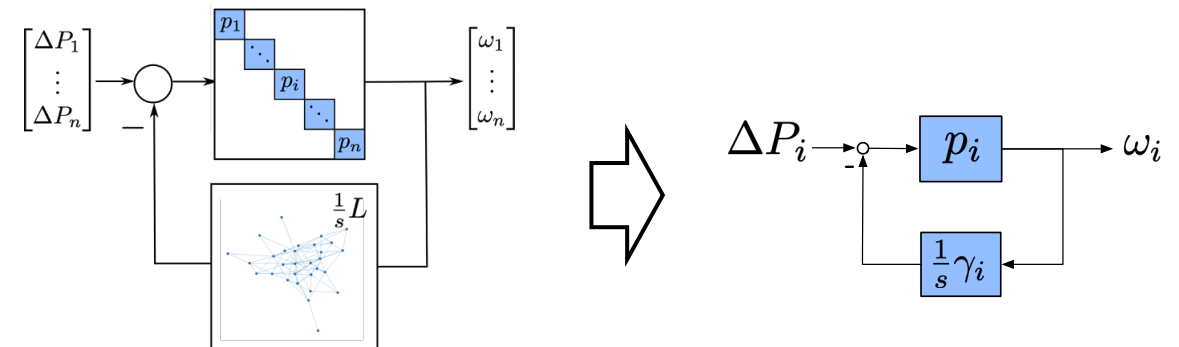


Pates & Mallada 2019

Assume: $p_i(s)$ is stable

Define: $h(s) \in PR$ (passive)

Test: If $h(s) \left(1 + \gamma_i \frac{1}{s} p_i(s)\right) \in SPR, \forall i$, then system stable for networks $[L']_{ii} \leq \frac{\gamma_i}{2}, \forall i$



Outline

- Merits and trade-offs of low inertia
 - Control Perspective: Lighter systems are easier to control!
- Scale-free Stability Analysis of Grids
 - Generalizes passivity notions using network information
- Grid Shaping Control
 - Grid-following/forming control framework for controlling future grids

Grid Shaping Control

Use model matching control to shape system response

Grid-following IBRs

Grid-forming IBRs

Grid-shaping with GFL IBRs [TPS 21]



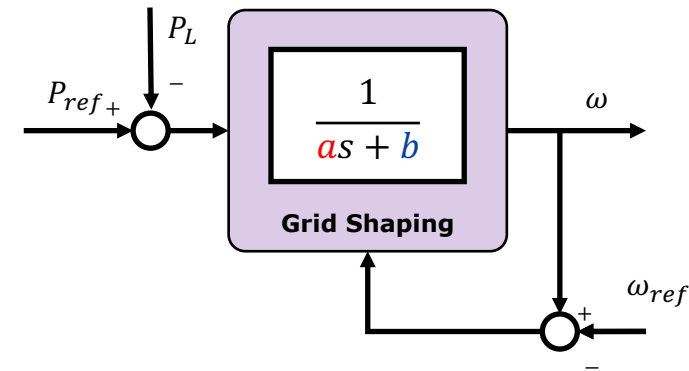
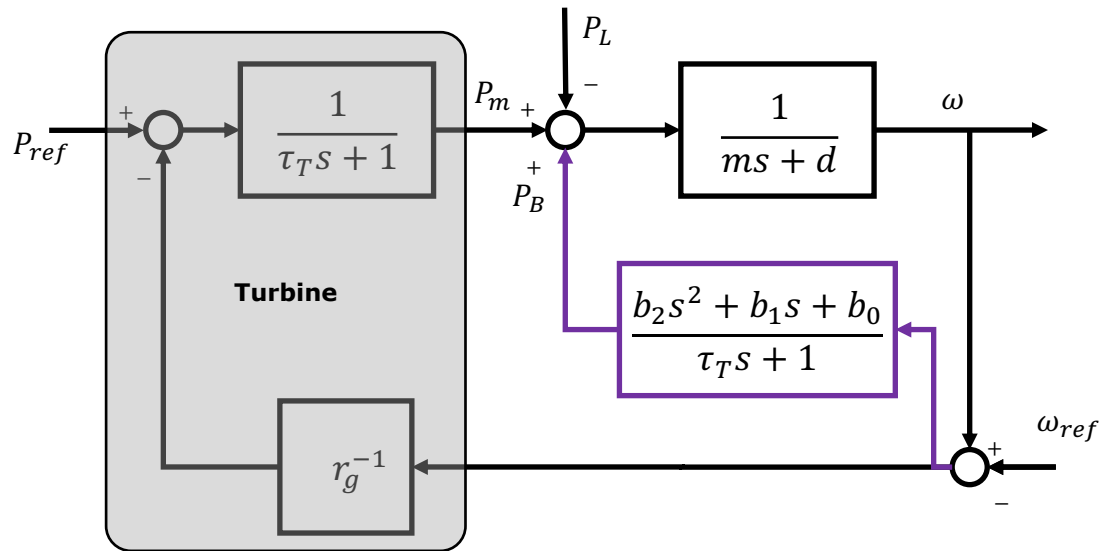
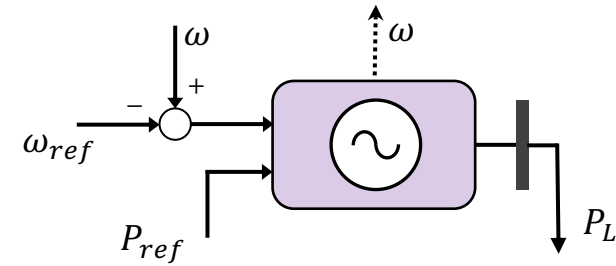
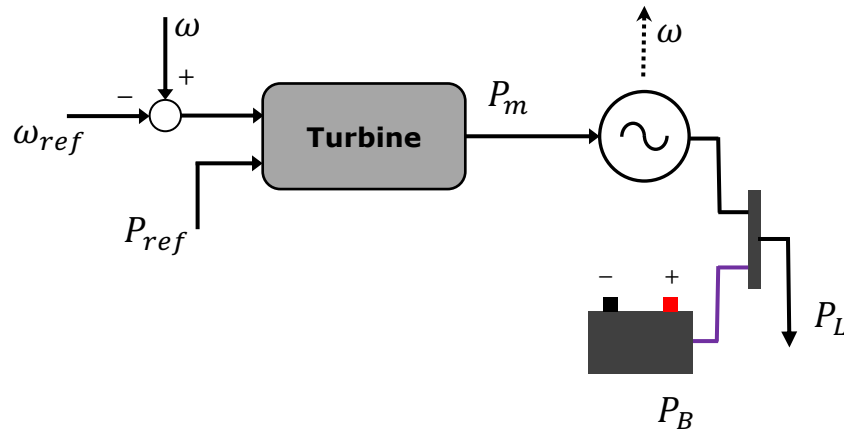
Yan Jiang



Eliza Cohn



Petr Vorobev



Tunable Performance:

$$\text{RoCoF} = \frac{1}{a} \Delta P, \quad \Delta \omega = \frac{1}{b} \Delta P$$

Grid-shaping with GFL IBRs [TPS 21]



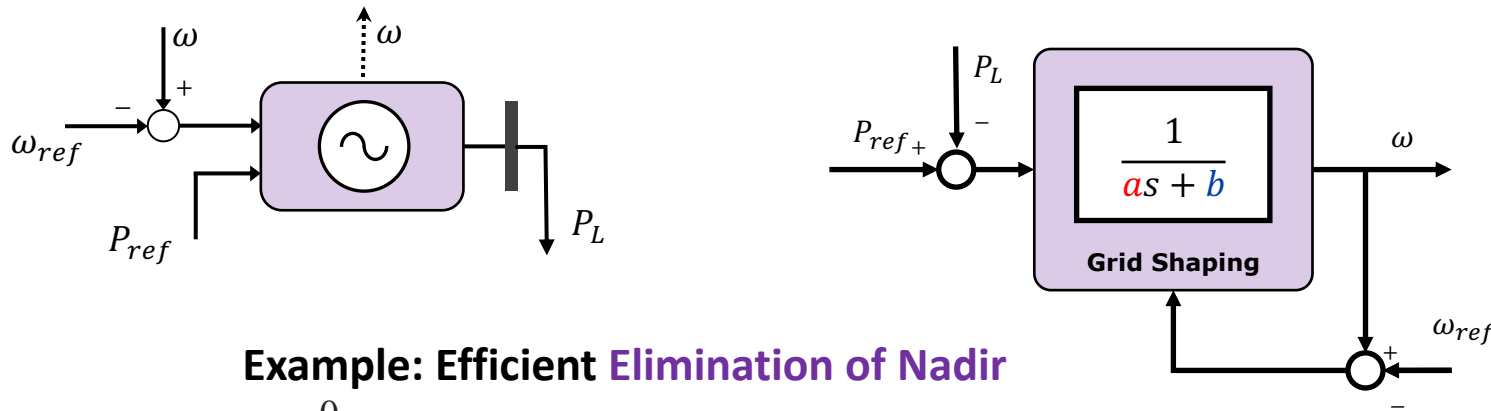
Yan Jiang



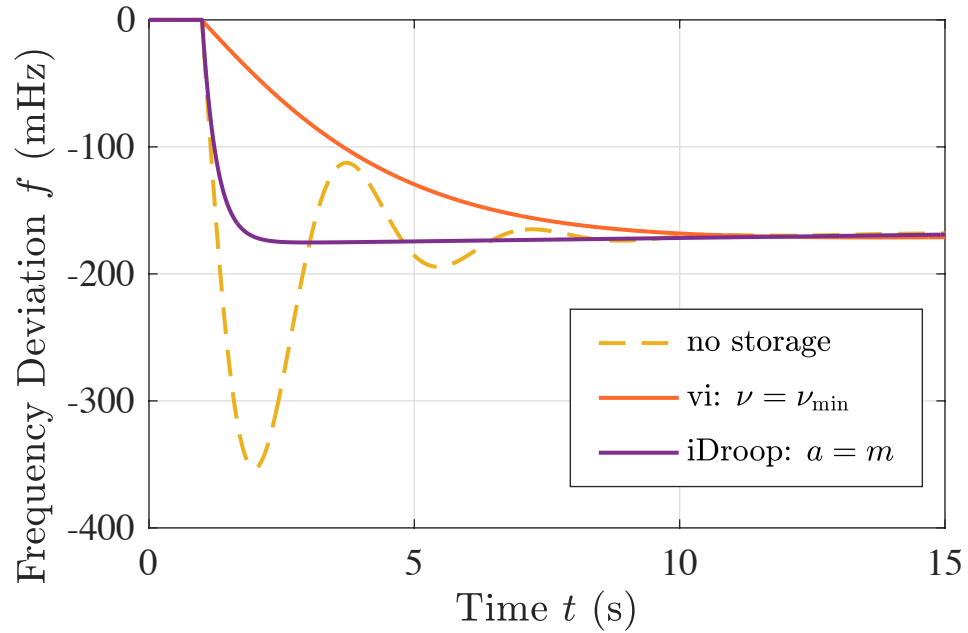
Eliza Cohn



Petr Vorobev

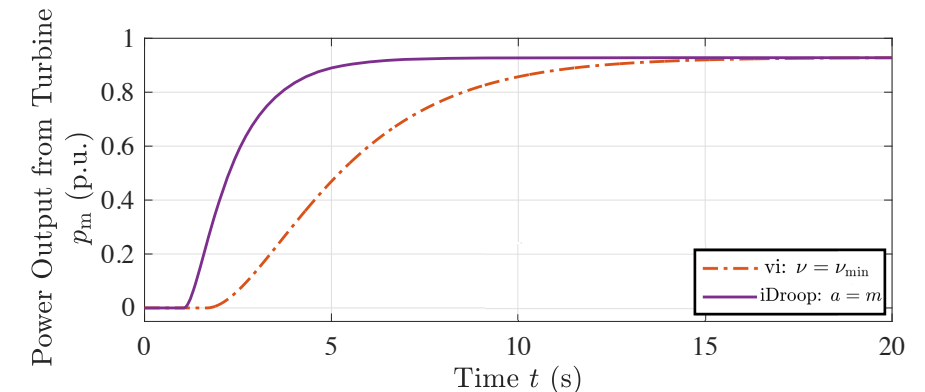
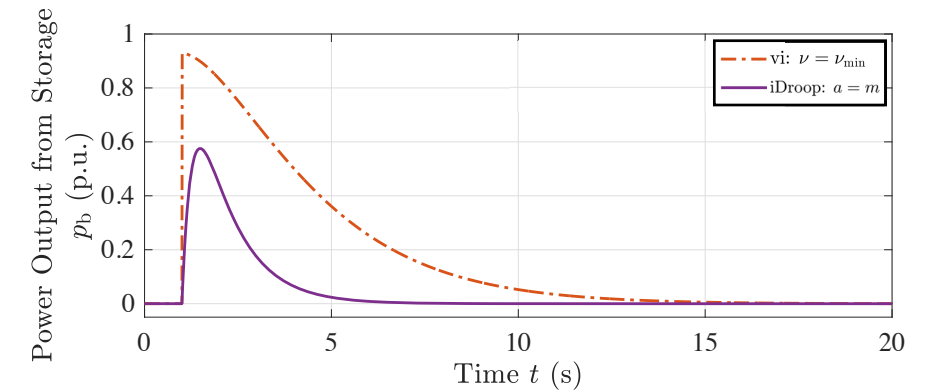


Example: Efficient Elimination of Nadir



Tunable Performance:

$$\text{RoCoF} = \frac{1}{a} \Delta P, \quad \Delta \omega = \frac{1}{b} \Delta P$$



Grid-shaping with GFL IBRs [TPS 21]



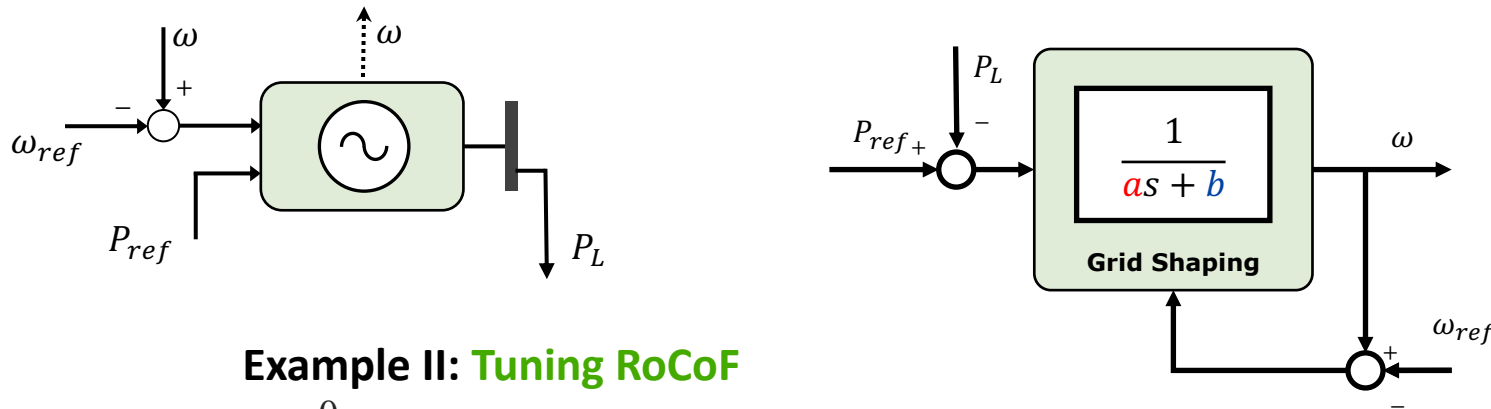
Yan Jiang



Eliza Cohn



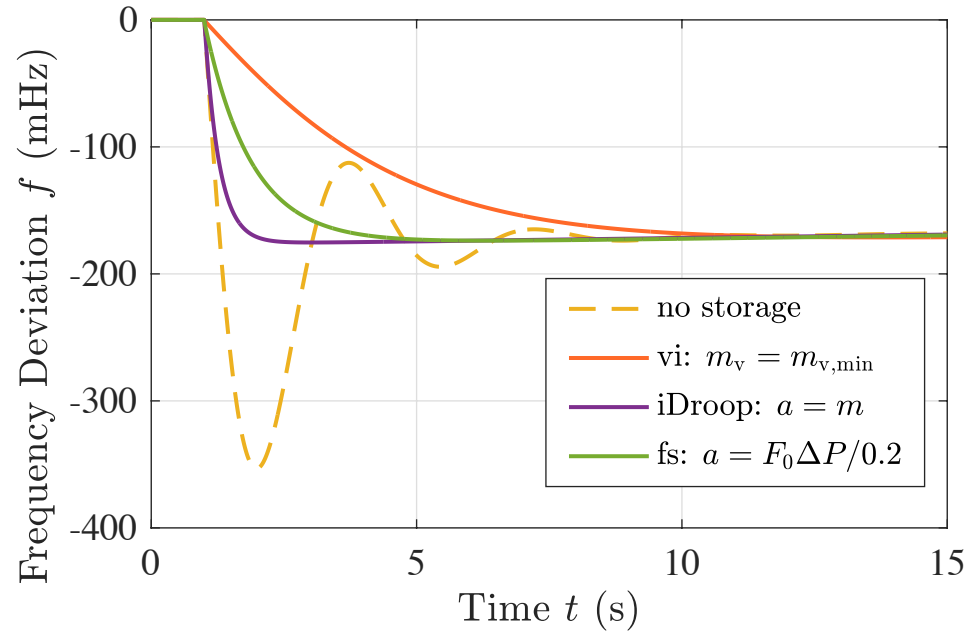
Petr Vorobev



Tunable Performance:

$$\text{RoCoF} = \frac{1}{a} \Delta P, \quad \Delta \omega = \frac{1}{b} \Delta P$$

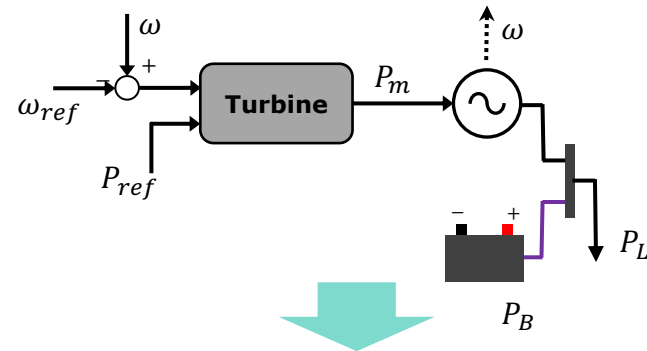
Example II: Tuning RoCoF



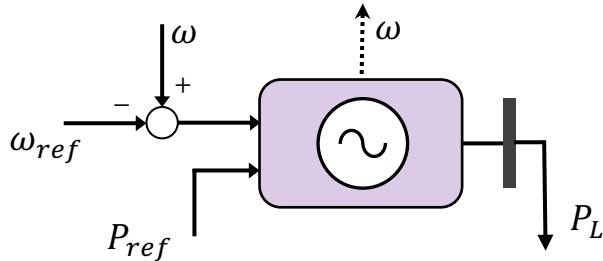
Grid Shaping Control

Use model matching control to shape system response

Grid-following IBRs



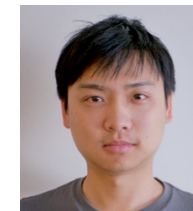
Grid-forming IBRs



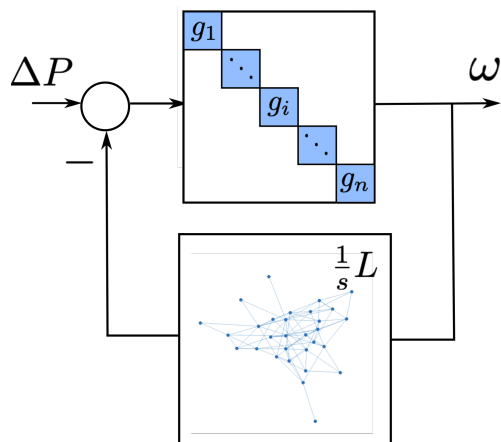
Tunable Performance:

$$\text{RoCoF} = \frac{1}{a} \Delta P, \quad \Delta \omega = \frac{1}{b} \Delta P$$

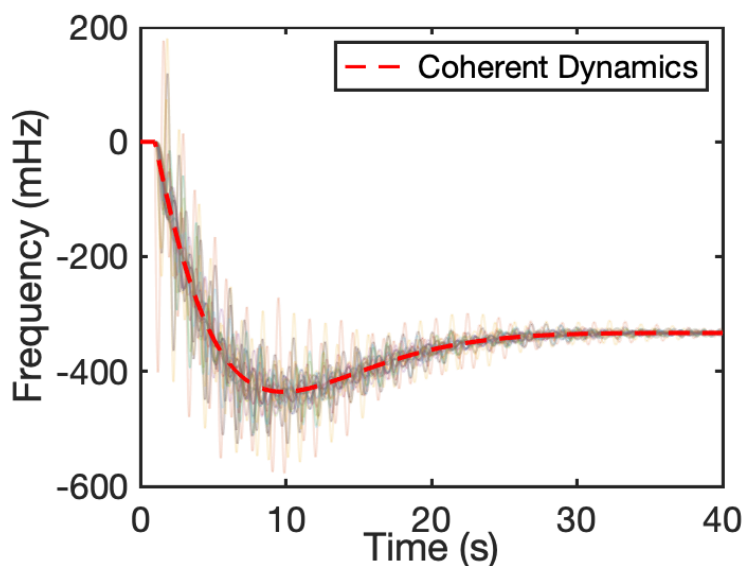
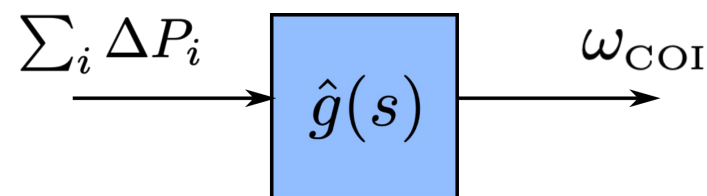
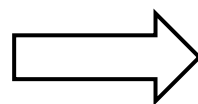
Generalized Center of Inertia (COI) [CDC 19, ArXiv 23]



Hancheng Min Richard Pates



What is the exact *response* of the *COI* of this network?



Generalized COI:

$$\hat{g}(s) = \left(\sum_{i=1}^n g_i^{-1}(s) \right)^{-1}$$

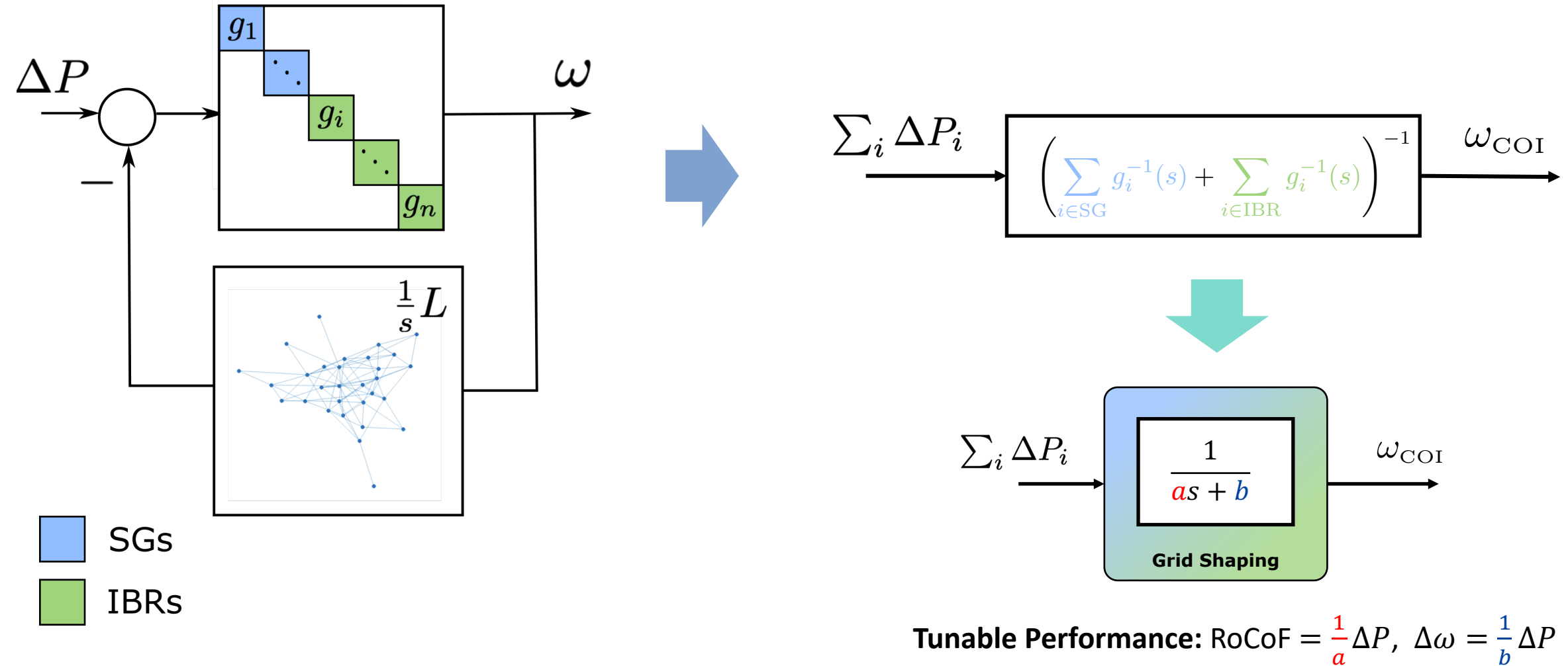
- **Properties of $\hat{g}(s)$:**
- Representation of aggregate response
- Accuracy of approximation:
 - is frequency dependent
 - increases with network connectivity
- Provides excellent template for reduced order models (via balance-truncations)

[CDC 19] Min, M. Dynamics concentration of large-scale tightly-connected networks. **Conference on Decision and Control 2019**

[ArXiv 23] Min, Pates, M. A frequency domain analysis of slow coherency in networked systems. arXiv:2302.08438, **2023, submitted**

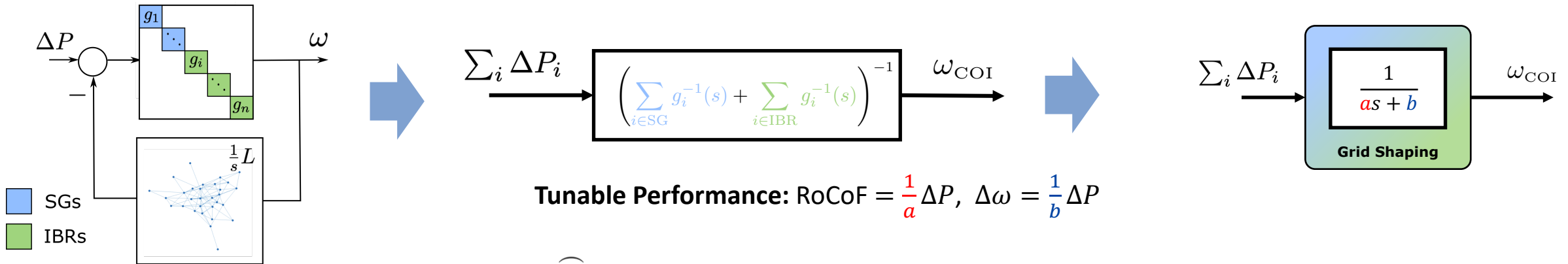


GFM System-wide Grid-shaping [LCSS 20]

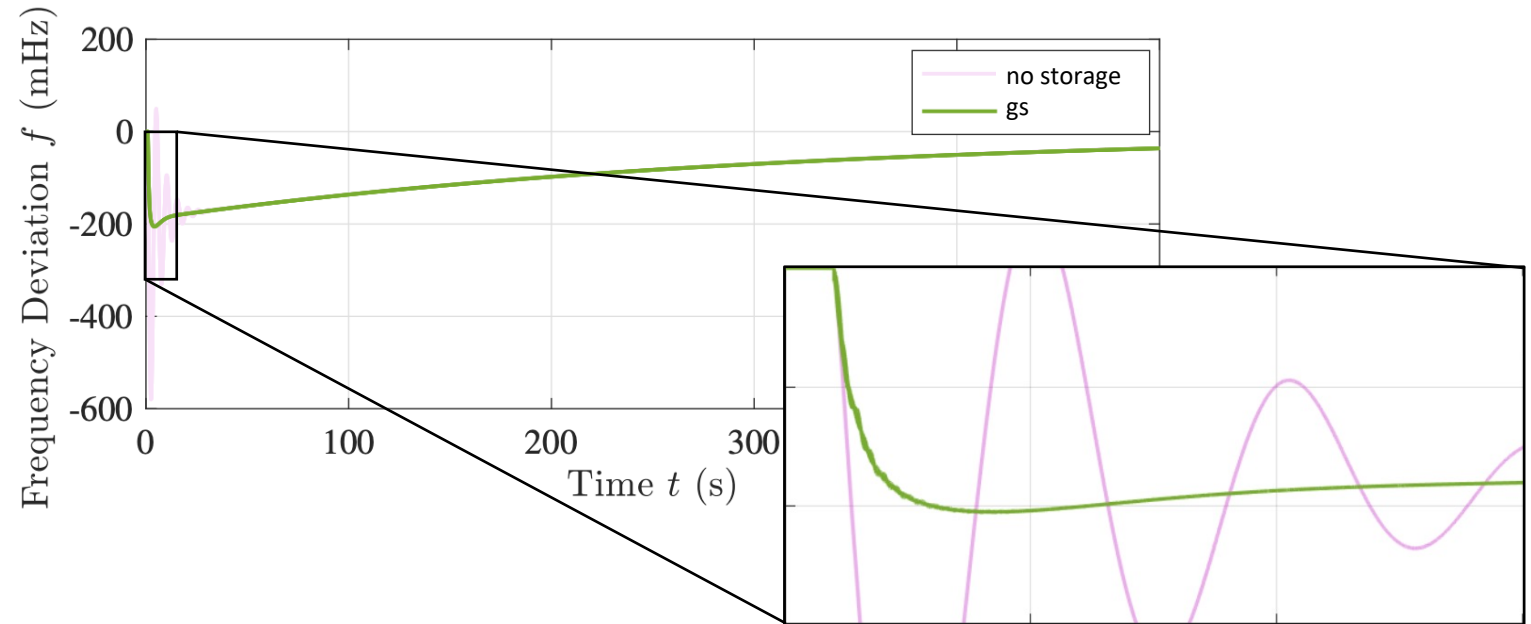
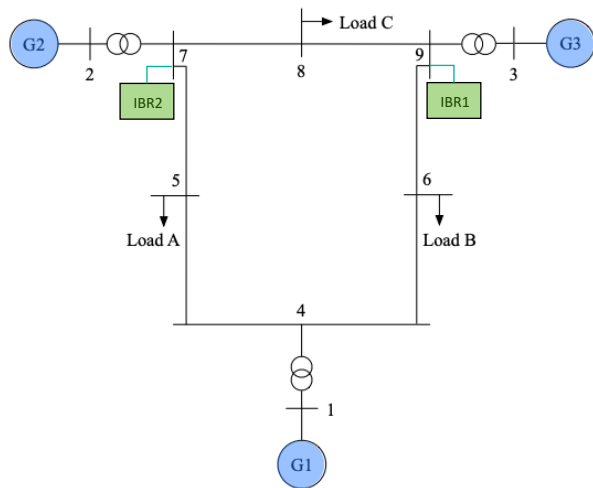




GFM System-wide Grid-shaping [LCSS 20]



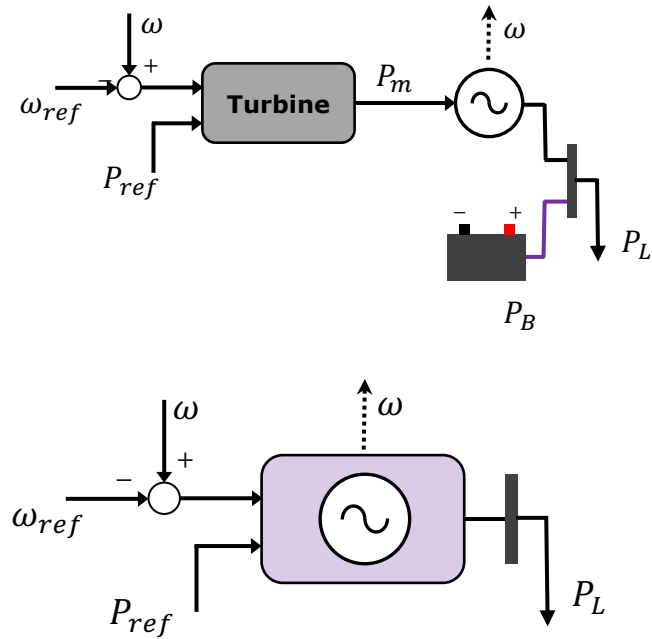
Tunable Performance: $\text{RoCoF} = \frac{1}{a} \Delta P$, $\Delta \omega = \frac{1}{b} \Delta P$



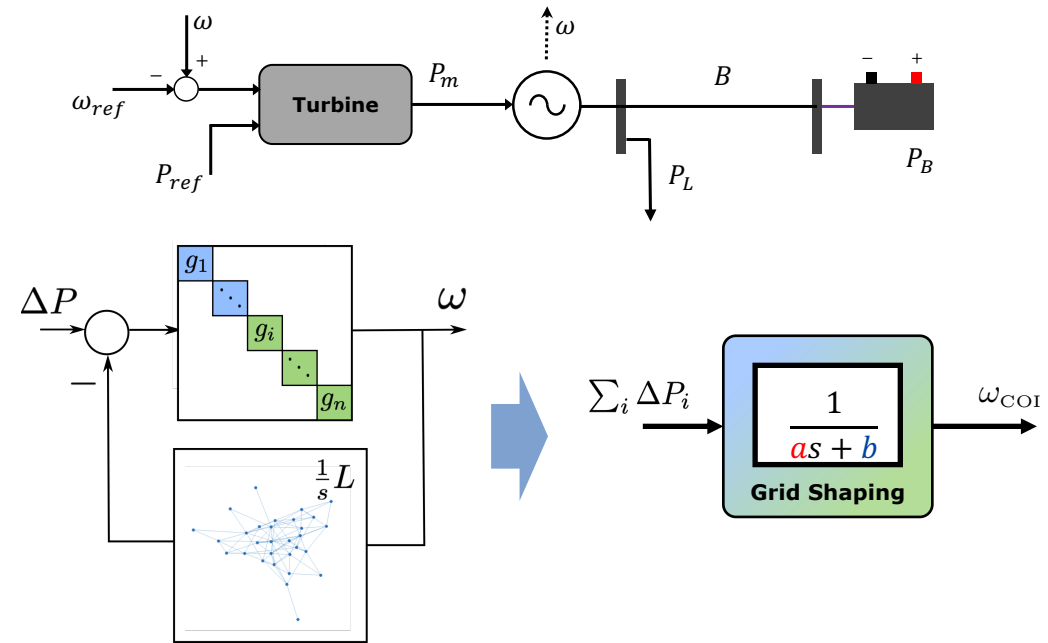
Grid Shaping Control

Use model matching control to shape system response

Grid-following IBRs



Grid-forming IBRs



Tunable Performance: $\text{RoCoF} = \frac{1}{a} \Delta P$, $\Delta\omega = \frac{1}{b} \Delta P$, τ' , ...

Summary

- **Merits and trade-offs of low inertia**
 - Control Perspective: Lighter systems are easier to control!
 - Smarter controller can provide multiple benefits in Nadir, RoCoF, inter-area oscillations, and disturbance rejection, with less effort
- **Scale-free Stability Analysis of Grids**
 - Generalizes passivity notions using network information
 - Decentralized test based on local models
 - Compatible with H_∞ -synthesis methods
- **Grid Shaping Control**
 - Grid-following/forming control framework for future grids
 - Leverages IBRs to *shape* the generalized COI response

Thanks!



Yan Jiang



Hancheng Min



Eliza Cohn



Petr Vorobev



Richard Pates



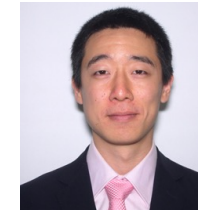
Fernando Paganini



Dominic Groß



Bala K. Poolla



Yashen Lin



Andrey Bernstein

Merits and trade-offs of low inertia

[TAC 21] Jiang, Pates, M, *Dynamic droop control in low inertia power systems*, **IEEE Transactions on Automatic Control**, 2021

Scale-free Stability Analysis

[TCNS 19] Pates, M. *Robust Scale Free Synthesis for Frequency Regulation in Power Systems*, **IEEE Transactions on Control of Network Systems**, 2019

Generalized Center of Inertia

[CDC 19] Min, M. Dynamics concentration of large-scale tightly-connected networks. **Conference on Decision and Control 2019**

[ArXiv 23] Min, Pates, M. A frequency domain analysis of slow coherency in networked systems. **arXiv:2302.08438 2023, submitted**

Grid Shaping Control

[LCSS 20] Jiang, Bernstein, Vorobev, M. Grid-forming frequency shaping control for low-inertia power systems **IEEE Control Systems Letters** 2020

[TPS 21] Jiang, Cohn, Vorobev, M. Storage-based frequency shaping control **Transactions on Power Systems** 2021

[LCSS 23] Poolla, Lin, Bernstein, M, Groß. Frequency shaping control for weakly-coupled grid-forming IBRs **IEEE Control Systems Letters** 2023